

# Taller Divulgativo en el CENIM

28 Enero 2014. 12:30 h  
Sala de Conferencias

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**María M. Aranda y Carlos Capdevila**

**Herramientas termodinámicas para el diseño de aleaciones metálicas. Modelización de diagramas de fase y su aplicación en el diseño de materiales metálicos**



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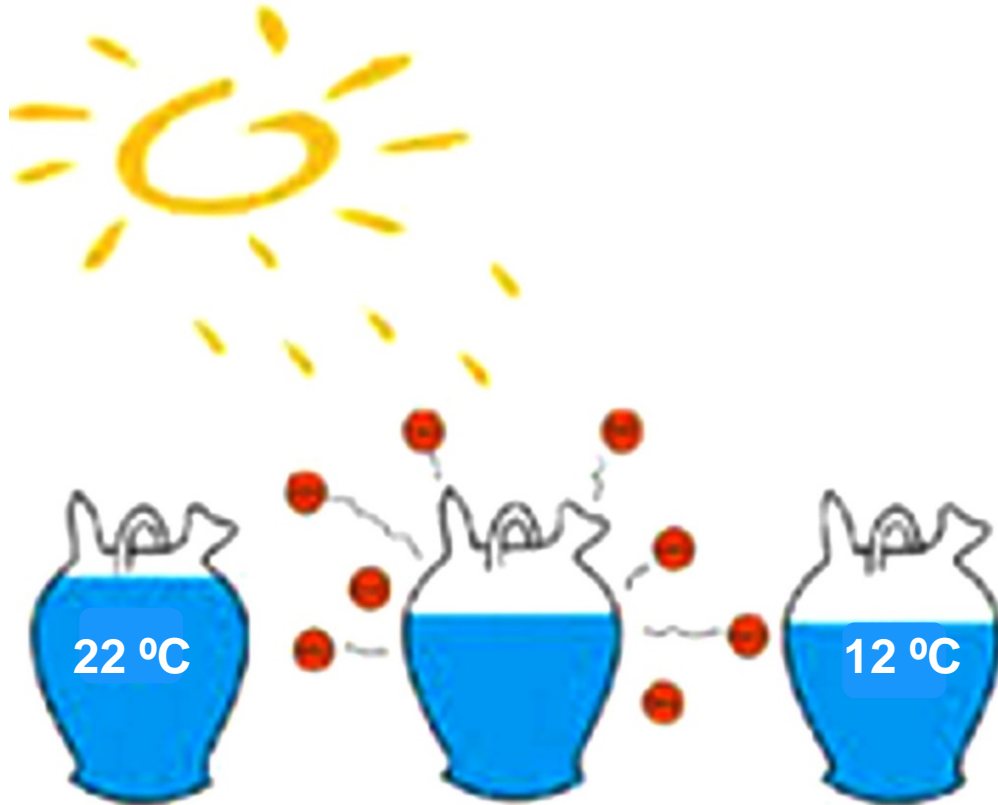
# PARTE I

Principios para el diseño de aleaciones  
metálicas por medio de herramientas  
termodinámicas



# Termodinámica y Diseño de Materiales

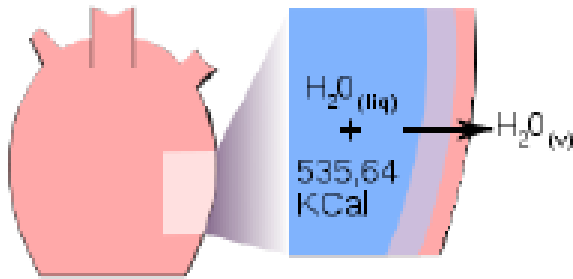
*Mecanismo del botijo*



- ☐ Selección de materiales en función de su aplicación
- ☐ Comportamiento durante la síntesis y el conformado
- ☐ Prever y analizar el comportamiento en condiciones de trabajo

# Termodinámica y Diseño de Materiales

## Mecanismo del botijo



- ❑ En 1995, Gabriel Pinto y José Ignacio Zubizarreta de la Universidad Politécnica de Madrid desarrollaron un modelo matemático para un botijo esférico.

$$-\frac{dV}{dt} = K' \cdot a(H_s - H)$$

$$V \cdot C_p \cdot \left(\frac{dT}{dt}\right) = h_c \cdot a \cdot (T_g - T_s) + f \cdot \epsilon \cdot \sigma \cdot (4\pi r^2 - s) \cdot [(273 + T_g)^4 - (273 + T_s)^4] - U \cdot a \cdot (T - T_s) - \lambda_w \cdot \left(\frac{dV}{dt}\right)$$

donde:

$V$  = volumen del agua

$t$  = tiempo

$C_p$  = capacidad calorífica del agua

$T$  = temperatura del agua

$T_g$  = temperatura del aire

$T_s$  = temperatura de la superficie del agua

$a$  = área de la superficie externa del agua

$4\pi r^2$  = área de la superficie total del botijo

$s$  = área del agua en contacto con el aire

$\lambda_w$  = calor de vaporización del agua

$h_c$  = coeficiente de convección

$f \cdot \epsilon \cdot \sigma$  = coeficiente de radiación de calor

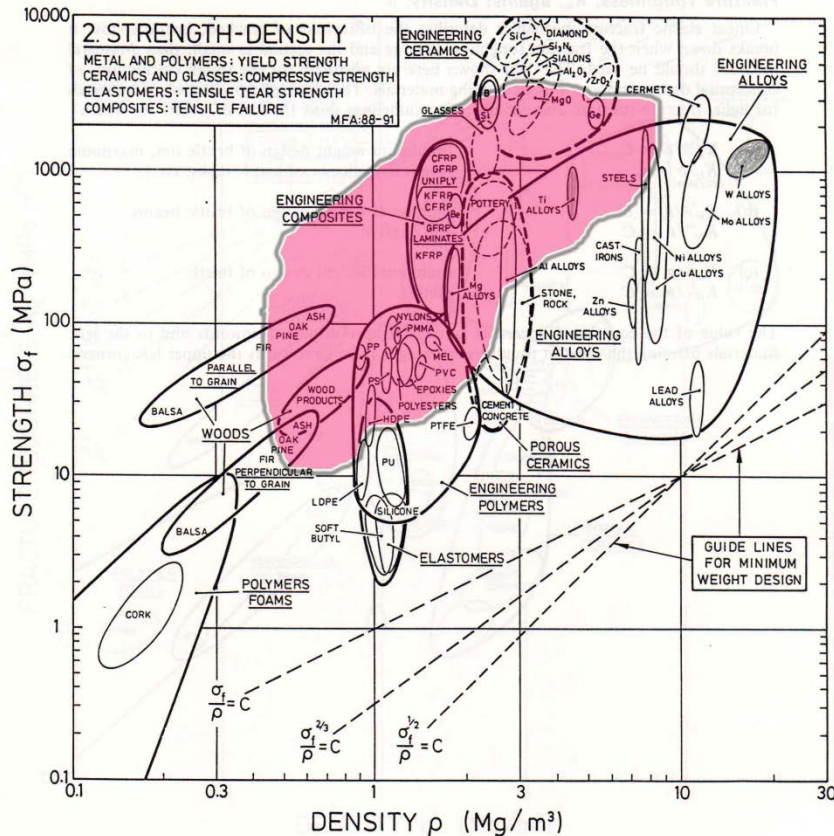
$U$  = coeficiente de transmisión de calor del agua

$K'$  = coeficiente de transferencia de masa para el agua

$H_s$  = humedad de saturación

$H$  = humedad del aire

# Termodinámica y Diseño de Materiales



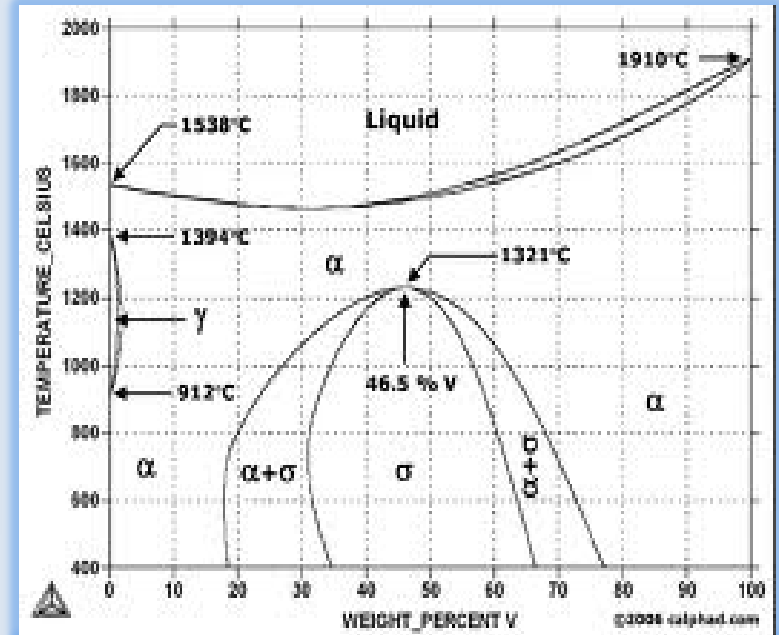
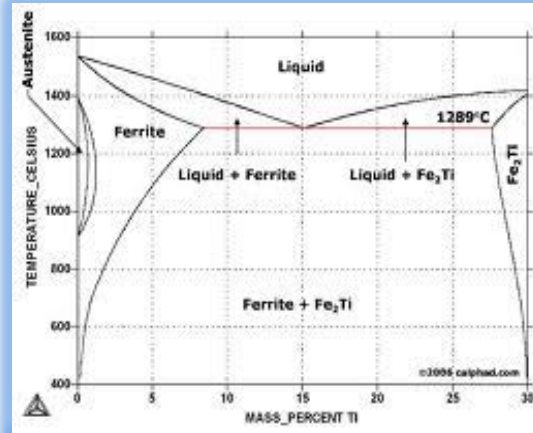
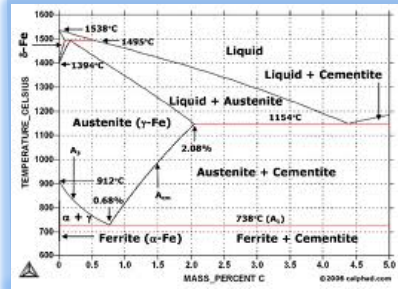
Michael Ashby, *Materials Selection in Mechanical Design*, 4th Edition, BH (2010)

- ❑ Los mapas de propiedades representan los distintos materiales en función de las propiedades que queremos buscar
- ❑ En una misma “familia”, como los metales, hay una gran variabilidad como consecuencia de la microestructura y de la presencia de distintas fases
- ❑ Necesitamos controlar las fases presentes en nuestra aleación, y lo hacemos mediante diagrama fases

## Diagrama de equilibrio de fases

- Representación de la combinación de fases estables en un sistema en función de  $T$ ,  $P$ ,  $E$ ,  $X$  y  $P_{\text{gas}}$

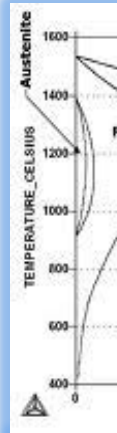
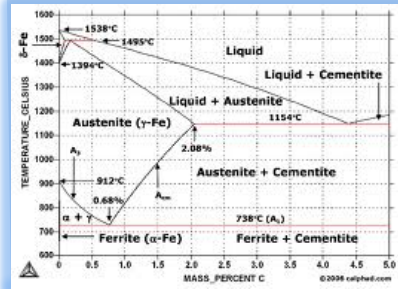
# Diagramas de Fase y Materiales Reales



- ❑ En los últimos 150 años se han ido acumulando datos experimentales que nos permiten tener una vasta colección de diagramas binarios y ternarios, que son las “fichas” para determinar condiciones de procesamiento (temperatura y presión) para obtener una determinada microestructura



# Diagramas de Fase y Materiales Reales



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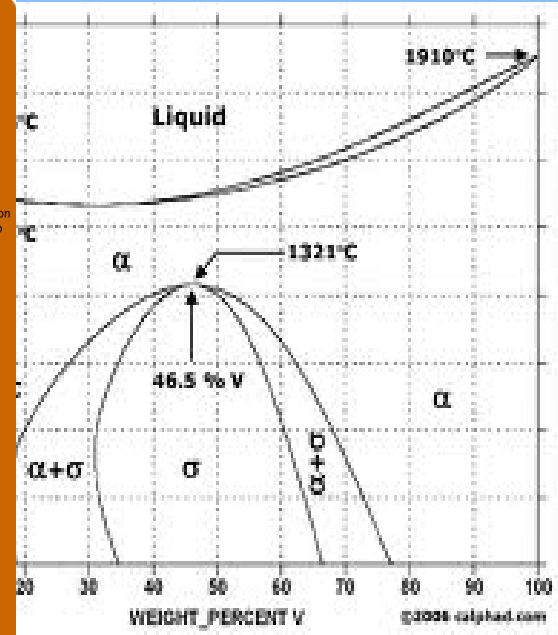
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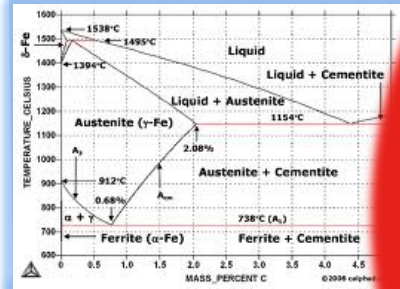
**Steels: Processing, Structure, and Performance**

**Steel Metallurgy for the Non-Metallurgist**



- ❑ En los últimos 150 años se han ido acumulando datos experimentales que nos permiten tener una vasta colección de diagramas binarios y ternarios, que son las “fichas” para determinar condiciones de procesamiento (temperatura y presión) para obtener una determinada microestructura

# Diagramas de Fase y Materiales Reales



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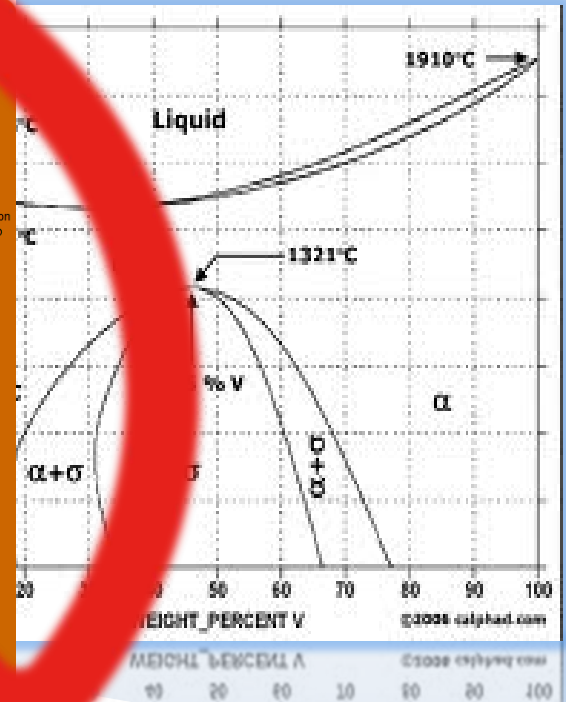
Elements of Metallurgy and Engineering Alloys

ASM Alloy Phase Diagram Database

Phase Diagrams for Binary Alloys, Second Edition

Handbook of Phase Diagrams (10 Volumes)

Steels: Processing, Structure, and Performance



¡ Sistemas Reales  $\leftrightarrow$  Sistemas Multicomponentes !

- ❑ Para estudiar este problema, hace 40 años se pusieron las bases por parte de Larry Kaufman and Himo Ansara de la metodología CALPHAD (**CAL**culacion of **PH**ase **D**iagrams)



# Breve reseña del método CALPHAD



- ❑ En los 70s científicos de ManLabs (USA); KIT (Suecia); Universidad de Grenoble (Francia) y NPL (Reino Unido) aplicaron el concepto de “lattice stabilities” para calcular  $\Delta G$  entre los distintos estados estables y metaestables de una fase como función de la temperatura, lo que permitía calcular de forma más precisa las fronteras de equilibrio entre las distintas fases de un sistema
- ❑ En 1979, los trabajos de CALPHAD cristalizaron en una base de datos denominada SGTE (Scientific Group Thermodata Europe), que contenía los datos experimentales recopilados hasta el momento para cientos de compuestos inorgánicos y aleaciones, y que por primera vez eran accesibles para toda la Comunidad Europea por medio del sistema de comunicaciones EURONET
- ❑ La base de datos SGTE es la matriz de todas las bases de datos posteriores implementadas dentro de los distintos softwares comerciales que trabajan con este método.

<http://www.calphad.org/>

The screenshot shows a Windows XP desktop environment. The taskbar at the bottom includes icons for Internet Explorer, Firefox, and several folders. The desktop background is a scenic image of a street. Various application icons are visible on the left and right sides of the desktop, including Subtitle Edit, Roxio Creator Home, Mp3tag, PowerISO, Adobe Acrobat X Pro, QuickTime Player, Freemake Video Converter, Cyberduck, Adobe Applications, ashby, MaterialBUIK-St..., 2012-IESF, Prensa, Prensa Cientific, ebooks, EndNote, calibre 64bit - E-book ma..., ViceVersa PRO, WOL ThermoCalc, Eudora, JuulJensen\_19..., ReX textures in cold rolled st..., ReX effect of stress, Larsen\_2003 JM..., hansen\_AM, and Microsoft Word 2010. A weather widget in the top right corner shows the temperature in Madrid as 10°C and the date as 27/01/2014.

The browser window displays the CALPHAD website. The page features a blue sidebar with a navigation menu and a main content area with a large heading and a paragraph of text.

**Navigation Menu (Left Sidebar):**

- Home
- Introduction
- Advisory Board
- Editorial Board
- Conference
- Journal
- CALPHAD Awards
- Links
- Contact us
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- CALPHAD in Wikipedia
- Announcements of Conferences and Positions
- Larry Kaufman

**Main Content Area:**

## CALPHAD

<http://www.calphad.org>

The design of industrial processes requires reliable thermodynamic data. CALPHAD (Computer Coupling of Phase Diagrams and Thermochemistry) aims to promote computational thermodynamics through development of models to represent thermodynamic properties for various phases which permit prediction of properties of multicomponent systems from those of binary and ternary subsystems, critical assessment of data and their incorporation into self-consistent databases, development of software to optimize and derive thermodynamic parameters and the development and use of databanks for calculations to improve understanding of various industrial and technological processes. This work is disseminated through the CALPHAD journal and its annual conference. Contributions of high quality in these and related fields, especially the fields of first-principles calculations, experimental measurements of thermochemical and phase equilibrium data, phase transformations, and the process and materials designs that the CALPHAD works are based on or used for, are welcome.

## ¿En que consiste el método CALPHAD?

**DIAGRAMA DE FASES:**  
Representación gráfica  
de la situación de  
equilibrio de un sistema

**EQUILIBRIO:**  
Configuración de fases  
que hace mínima la  
energía libre de Gibbs  
(G) del sistema

El cálculo de diagramas de  
equilibrio de fases se basa en el  
cálculo de G de las fases del sistema

# ¿En que consiste el método CALPHAD?

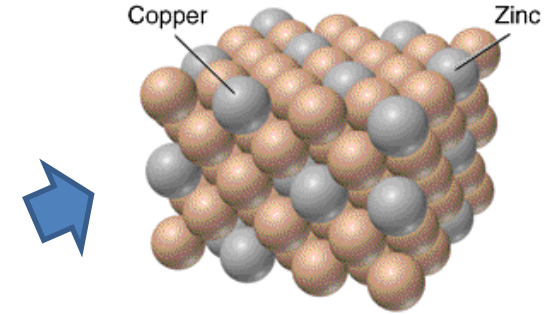
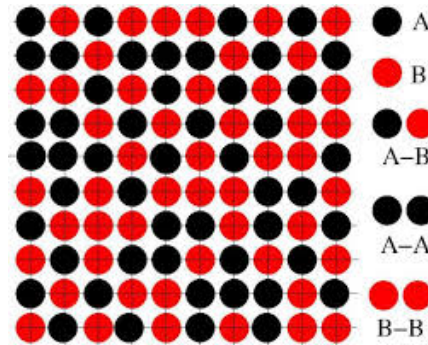


# Determinación de una expresión para G

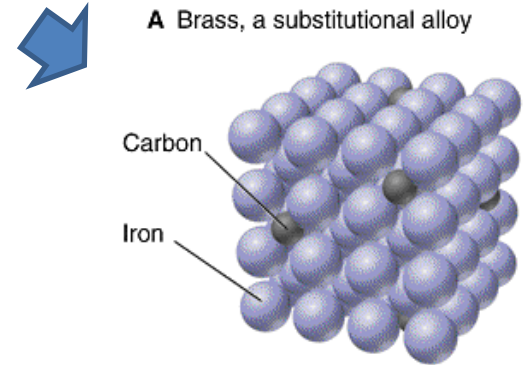
- ❑ Encontrar una expresión matemática que describa G en función de las propiedades fisico-químicas de la fase

Sistemas sencillos → sustitución aleatoria

Modelo de Bragg-Williams →



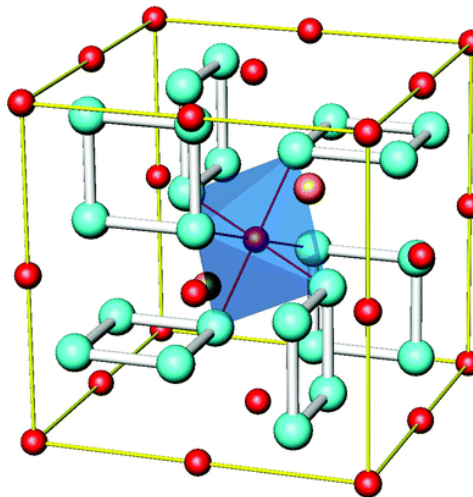
A Brass, a substitutional alloy



B Carbon steel, an interstitial alloy

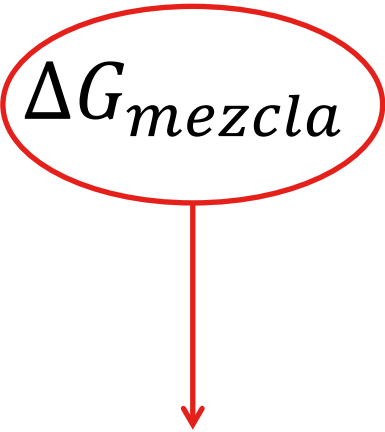
Sistemas complejos → modelo sub-redes

Vista de la estructura de  $\text{Mo}_3\text{Sb}_7$





## Determinación de una expresión para G

$$\Delta G_{sistema} = \sum_{i=2}^n x_i \Delta G_i^0 + \Delta G_{mezcla}$$


$$\Delta G_{mezcla} = \Delta H_{mezcla} - T \Delta S_{mezcla}$$


**Sistemas ideales**



$$\Delta H_{mezcla} = 0$$

**Sistemas reales**



$$\Delta H_{mezcla} \neq 0$$



# Determinación de una expresión para G

Por ejemplo, de forma mas particular para un sistema bifasico, la expresion de G:

$$G = x_A G_A + x_B G_B + \Delta G_{\text{mix}}$$

$$\Delta G_{\text{mix}} = \Delta H_{\text{mix}} - T \Delta S_{\text{mix}} = \Delta H_{\text{mix}} + RT(x_A \ln x_A + x_B \ln x_B)$$

## Soluciones ideales:

$\Delta H_{\text{mix}} = 0$  (energía interna del sistema antes y después de la mezcla)

$$G = x_A G_A + x_B G_B + RT(x_A \ln x_A + x_B \ln x_B)$$

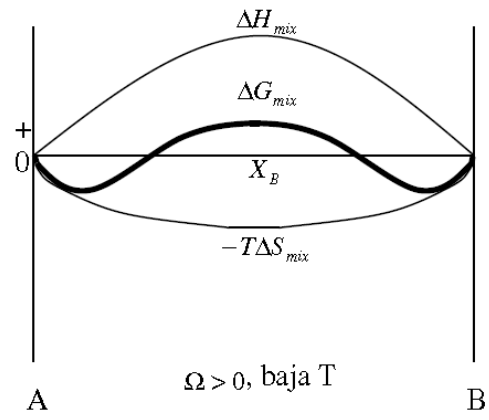
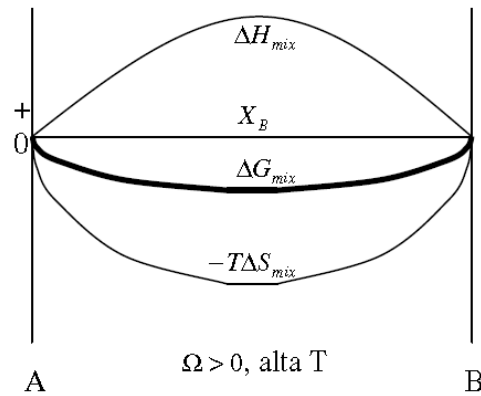
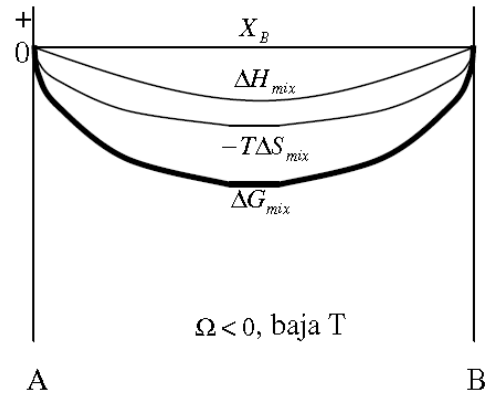
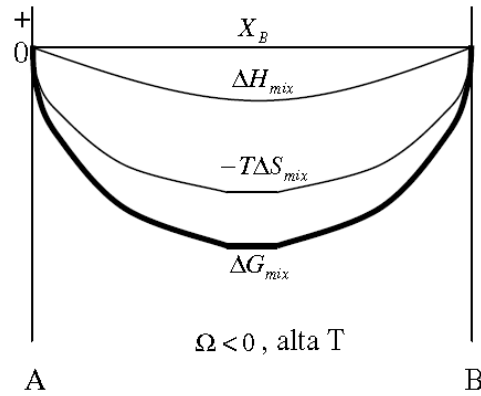
## Soluciones reales:

$\Delta H_{\text{mix}} \neq 0$  (en sistemas reales hay calor absorbido o generado durante la mezcla)

$$G = x_A G_A + x_B G_B + \Omega x_A x_B + RT(x_A \ln x_A + x_B \ln x_B)$$

Modelo **cuasi-químico** o de soluciones regulares, donde la entalpia es debido a la energía de enlace entre los átomos vecinos que constituyen una fase

# Determinación de una expresión para G



# Determinación de una expresión para G

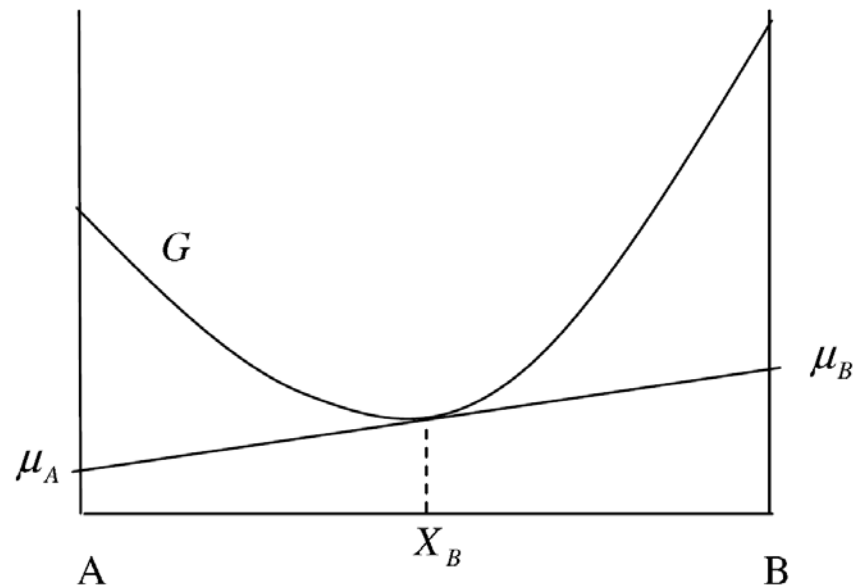
¿Cómo evaluamos la composición química de los elementos que forman una fase?

Potencial químico de A       $\mu_A = \left( \frac{\partial G}{\partial n_A} \right)_{T,P,n_B}$       Variación de la G al añadir una cantidad  $n$  del elemento A a la fase

$$G \text{ (molar)} = \mu_A x_A + \mu_B x_B$$

$$\mu_A = G_A + RT \ln x_A$$

$$\mu_B = G_B + RT \ln x_B$$



# Determinación de una expresión para G

¿Cómo evaluamos la composición química de los elementos que forman una fase?

Actividad de A       $\mu_A = G_A + RT \ln a_A$

Diferencia entre el valor de G y el del  $\mu$  del elemento A en la fase

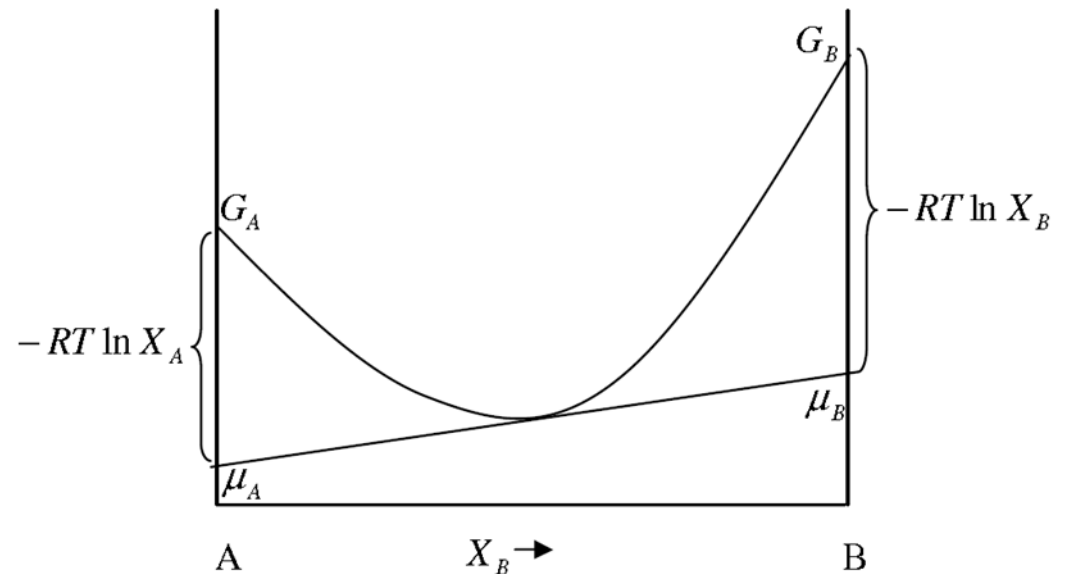
$$\mu_A = G_A + RT \ln a_A$$

$$\mu_B = G_B + RT \ln a_B$$

Soluciones reales:

$$\ln \left( \frac{a_A}{x_A} \right) = \frac{\Omega}{RT} (1 - X_A)^2$$

$$\ln \left( \frac{a_B}{x_B} \right) = \frac{\Omega}{RT} (1 - X_B)^2$$



Soluciones ideales,  $\Omega=0 \rightarrow a_A = x_A ; a_B = x_B$

# Determinación de una expresión para G

- A medida que suponemos mas interacciones entre los componentes, vamos considerando modelos mas complejos. Así, de soluciones regulares pasamos al modelo que se usa en CALPHAD mas habitualmente que es el sub-regular.

## Solución ideal:

$$\Delta G_{mezcla} = 0$$

## Solución regular:

$$\Delta G_{mezcla} = x_A \cdot x_B \cdot \left[ L_{A-B}^{0,0,1} + L_{A-B}^{0,1,f} \cdot T \right]$$

## Solución sub – regular:

$$\Delta G_{mezcla} = x_A \cdot x_B \cdot \left[ L_{A-B}^{0,0,1} + L_{A-B}^{0,1,f} \cdot T + (L_{A-B}^{1,0,1} + L_{A-B}^{1,1,f}) \cdot (x_A - x_B) \right]$$

Sol. Diluidas > Sol. Ideales > Sol. Regulares > Sol. sub-Regulares

Mayor interacción entre los componentes

## Creación de una BBDD consistente

- ❑ Ajustar una expresión de  $\Delta G_{\text{sistema}}$  bajo un modelo de soluciones sub-regulares a los datos experimentales para poder determinar los coeficientes que son desconocidos
- ❑ Una vez hecho esto, ya podemos describir matemáticamente nuestro sistema
- ❑ Conseguimos una base de datos consistente
- ❑ ¿Y eso qué es?
  1. Pues que tenemos todos los datos en el mismo rango de Temperatura, Presión y composición de validez definido
  2. Descripción continua en especies para el rango de composición definido



## Software comercial

- ❑ Suites comerciales compuestas de una interface y bases de datos:



Compiten en:

- Dimensión de la base de datos y numero de sistemas incluidos
- El método de ajuste de la función G a los valores experimentales
- Modelos que se usan para describir las fases

# Software comercial

## ThermoCalc

Windows  
TCFE7®

### PROs

- 1. Fácil de usar
- 2. Muy versátil
- 3. Módulos adicionales para difusión (DICTRA) y precipitación (PRISMA)
- 4. BBDD continua actualización

### CONs

- 1. Muy caro!
- 2. Complicado en la programación
- 3. Poco versátil en la exportación de resultados

## MTDATA

Linux  
MTSOL®

### PROs

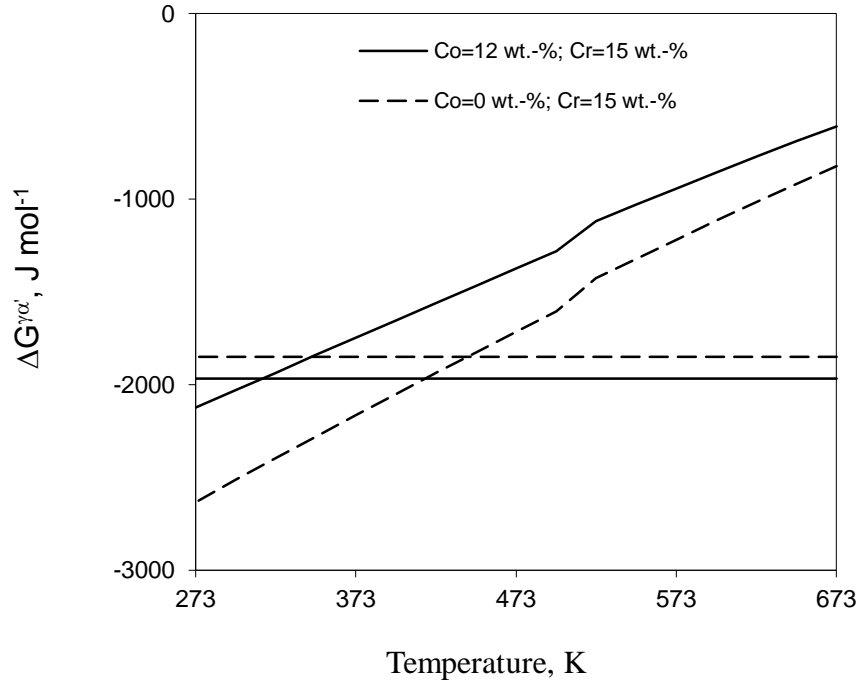
- 1. Fácil de usar
- 2. Sistemas cerámicos en la BBDD
- 3. Interface sencilla
- 4. Modo esclavo en otros programas F77 o F90

### CONs

- 1. Poco versátil
- 2. Modo grafico bastante deficiente

# Ejemplos

## Determinación temperatura Ms en Fe-0.4C-x<sub>1</sub>Co-x<sub>2</sub>Cr



Critical value in J mol<sup>-1</sup> of the driving force needed to trigger martensitic transformation:

$$\begin{aligned}
 -\Delta G_C^{\gamma\alpha'} = & 683 + 4009c_C^{0.5} + 1879c_{Si}^{0.5} + 1980c_{Mn}^{0.5} + 172c_C^{0.5} + 1418c_{Mo}^{0.5} + 1868c_{Cr}^{0.5} \\
 & + 1618c_V^{0.5} + 752c_{Cu}^{0.5} + 714c_W^{0.5} + 1653c_{Nb}^{0.5} + 3097c_N^{0.5} - 352c_{Co}^{0.5}
 \end{aligned}$$

## Determination of Ms Temperature in Steels: A Bayesian Neural Network Model

C. CAPDEVILA, F. G. CABALLERO and C. GARCÍA DE ANDRÉS

Department of Physical Metallurgy, Centro Nacional de Investigaciones Metalúrgicas (CENIM), CSIC, Avda. Gregorio del Amo, 8, 28040 Madrid, Spain. E-mail: cgd@cenim.csic.es

(Received on March 15, 2002; accepted in final form on May 13, 2002)

The knowledge of the martensite start (Ms) temperature of steels is sometimes important during parts and structures fabrication, and it can not be always properly estimated using conventional empirical methods. The additions in newly developed steels of alloying elements not considered in the empirical relationships, or with compositions out of the bounds used to formulate the equations, are common problems to be solved by experimental trial and error. If the trial process was minimised, cost and time might be saved. This work outlines the use of an artificial neural network to model the calculation of Ms temperature in engineering steels from their chemical composition. Moreover, a physical interpretation of the results is presented.

KEY WORDS: neural network analysis; martensite; modelling phase transformation; steels.

### 1. Introduction

The Ms temperature is of vital importance for engineering steels. Hence great efforts have been made in predicting the Ms temperature of these steels. Obviously, chemical composition of steel is the main factor affecting its Ms although the austenitising state, external stresses and stored deformation energy may sometimes play an important role as well. Martensite start temperature are usually relatively easy to calculate as long as the steels have a low alloy content.<sup>1-6</sup> Even though empirical equations exist for high alloy steels, they are not sufficiently general and are known to provide inaccurate answers for the new steels which contain different alloying elements, or their compositional range are out of bounds of those used to formulate the equations.

For instance, the interest of copper additions to the chemical composition of steels has increased in the last years. Copper-bearing low carbon steels are used in heavy engineering applications which demand a combination of strength, toughness and weldability.<sup>7-10</sup> Strength is achieved by precipitation of fine copper precipitates during ageing, instead of precipitation of carbide particles.<sup>11</sup> Therefore, copper is not in this respect different from any secondary hardening element in steels. Likewise, it has been demonstrated that copper sulphide strongly enhance acicular ferrite formation, which induces a good combination of mechanical properties as compared to bainite and especially to ferrite-pebble microstructures.<sup>12-15</sup> Likewise, power stations are nowadays designated to operate with steam temperatures in excess of 873 K. The steels currently being developed to cope with these requirements contain a total solute concentration which is often in

excess of 14 wt%. The main solutes include carbide forming elements such as chromium and molybdenum. Chromium also provides the necessary corrosion and oxidation resistance for prolonged elevated temperature service. The main alloys under consideration include numerous variants of the classical 12Cr-1Mo and 9Cr-1Mo steels.<sup>16,17</sup> These alloys have a high hardenability and a microstructure which is predominantly martensitic on cooling from the austenitising temperature. Their martensite start Ms temperature is therefore of considerable importance in deciding on the exact welding conditions necessary to avoid cracking.<sup>18</sup> An important variant of the 9Cr-1Mo steel is that in which tungsten is added to induce precipitation hardening.<sup>19</sup>

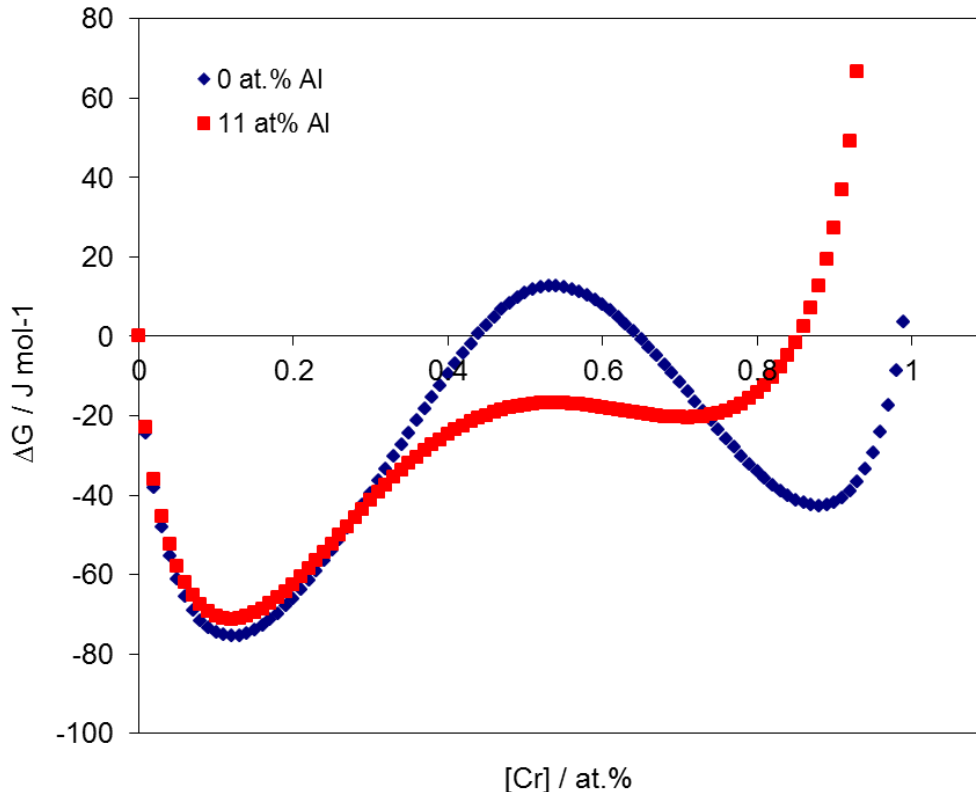
Gustafson and Ågren<sup>19</sup> reported that Co has a remarkable influence on coarsening of M<sub>23</sub>C<sub>6</sub> carbides in the 9Cr-1Mo steel. Their results show that a final average radius of the carbides after 50 000 h at 873 K decreases in 30% with a Co addition of 1.0 mass%. This raises the Creep stress with 30%. Moreover, it is assumed that slower particle coarsening also leads to a retard in the coarsening of the martensite lath structure. Thus, an improvement on creep life of the steels is expected.<sup>19</sup>

Likewise, it has been reported that the combined additions of cobalt and tungsten to the chemical composition strengthen the steel by precipitation of tungsten-cobalt (WC-Co) cemented carbides.<sup>20</sup> These new steels are widely used as tool steels where a good combination between abrasion resistance and corrosion resistance is required.<sup>21-23</sup>

It is then followed that the investigation of how copper, tungsten, and cobalt additions may affect the Ms temperature is an important issue. Thus, the aim of this work is to

# Ejemplos

## Descomposición spinodal en el sistema Fe-Cr-Al-Ti



$\Delta G_{mezcla}$  en el sistema Fe-Cr-Al-0.5Ti



Available online at [www.sciencedirect.com](http://www.sciencedirect.com)

SciVerse ScienceDirect

Acta Materialia 60 (2012) 4673–4684



[www.elsevier.com/locate/actamat](http://www.elsevier.com/locate/actamat)

### Phase separation kinetics in a Fe–Cr–Al alloy

C. Capdevila<sup>a,\*</sup>, M.K. Miller<sup>b</sup>, J. Chao<sup>a</sup>

<sup>a</sup> *Materalia Group, Centro Nacional de Investigaciones Metalúrgicas (CENIM-CSIC), Avenida Gregorio del Amo, 8, 28040 Madrid, Spain*

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Available online 26 June 2012

#### Abstract

The  $\alpha$ - $\alpha'$  phase separation kinetics in a commercial Fe–20 wt.% Cr–6 wt.% Al oxide dispersion-strengthened PM 2000™ steel have been characterized with the complementary techniques atom probe tomography and thermoelectric power measurements during isothermal aging at 673, 708, and 748 K for times up to 3600 h. A progressive decrease in the Al content of the Cr-rich  $\alpha'$  phase was observed at 708 and 748 K with increasing time, but no partitioning was observed at 673 K. The variation in the volume fraction of the  $\alpha'$  phase well inside the coarsening regime, along with the Avrami exponent 1.2 and activation energy 264 kJ mol<sup>−1</sup>, obtained after fitting the experimental results to an Austin–Rickett type equation, indicates that phase separation in PM 2000™ is a transient coarsening process with overlapping nucleation, growth, and coarsening stages.

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**Keywords:** Phase separation; Ferrous alloy; Mechanical alloying; Tomography; Thermoelectric power

#### 1. Introduction

The Fe–Cr–Al oxide dispersion-strengthened (ODS) ferritic steels are manufactured by a complex powder metallurgy route. Due to their high creep rupture strength and excellent swelling resistance many ODS ferritic steels are under development for several types of nuclear reactors, such as sodium fast reactors (SFR) or supercritical water reactors (SCWR) [1,2]. In such applications these alloys face severe embrittlement problems because their service temperature is in the range 373–823 K. In this temperature range the response of the materials to extreme conditions (high temperatures and irradiation resulting in swelling and corrosion) is partly determined by the extent of  $\alpha$ / $\alpha'$  phase separation. Thus, in the last few years binary Fe–Cr model alloys have been the focus of significant basic research [3–8].

In the present study atom probe tomography (APT) and thermoelectric power (TEP) measurements were used to

monitor the kinetics of Cr diffusion during the  $\alpha$ / $\alpha'$  phase separation process. APT is a unique technique that provides highly accurate quantitative data regarding the evolution of phase composition, size, morphology, and number density in the nm scale range during  $\alpha$ / $\alpha'$  phase separation. TEP provides macroscopic volumetric information on the response of a material to aging treatments and is also a powerful method to study the dissolution process of carbides in steels, as this technique is very sensitive to the number of atoms in solid solution in iron [9,10]. Therefore, the combination of TEP and APT was used to determine not only the composition of the phases involved, but also the kinetic parameters needed to characterize  $\alpha$ / $\alpha'$  phase separation during aging (isothermal heat treatment) of PM 2000™ ODS alloy.

Isothermal reactions allow a detailed analysis of  $\alpha'$  phase precipitation kinetics from a direct fit of the data to the Johnson–Mehl–Avrami–Kolmogorov (JMAK) [11–13] and Austin–Rickett (AR) [14] relations. From these analyses kinetic parameters, such as the so-called Avrami exponent and the activation energy, can be calculated to provide a significant understanding of the nucleation and growth processes of  $\alpha'$  precipitates.

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## New approach for the bainite start temperature calculation in steels

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The bainite start temperature  $B_s$  is defined as the highest temperature at which ferrite can transform by a displacive transformation. A common observation is that the bainite start temperature is very sensitive to the chemical composition, indicating that the influence of solutes is more than just thermodynamic. Empirical linear regression models have long been used to calculate the  $B_s$  in a limited range of compositions. This paper attempts to create an empirical model of wider applicability and higher accuracy by means of neural networks. The results are compared with those calculated using the thermodynamic theory for bainite transformation, revealing that in general this theory agrees with the experimental results, but some discrepancies can still be found when the alloys are heavily alloyed.

**Keywords:** Bainite start temperature, Neural network, Bayesian framework, Thermodynamics theory

### Introduction

Because of its mechanical properties and low cost, bainitic steel is being increasingly used in a number of industrial applications, ranging from rails to formula one gearboxes. The bainitic structure develops at temperatures between that for pearlite formation and the martensite start temperature. The exact value of these temperatures depends strongly on the elements present in the steel, and considerable work has been devoted to developing quantitative models for their compositional dependency. Early approaches for predicting the bainite  $B_s$  and the martensite start  $M_s$  temperatures essentially consisted of the fitting of simple linear empirical relationships.<sup>1-9</sup> Though easily communicated and interpreted, such methods often have very limited ranges of applicability because of their inability to grasp interactions or nonlinear effects. With the development of calculation frameworks such as CALPHAD, which allow prediction of thermodynamic properties of complex systems from data collected on simpler ones, more physically relevant approaches relying on the satisfaction of some thermodynamic criterion have gained importance.<sup>10,11</sup> These are briefly introduced in the next section. In general, such models extrapolate considerably better than the early empirical approaches. However, they suffer a number of drawbacks:

- (i) being essentially self-consistent, these approaches require that identical thermodynamic

databases are used in the predictions as those which were used for the derivation of the criteria. With the multiplication of databases (SGTE SSOL, NPL plus, TCFE, Kmart), this is increasingly becoming a problem. Recent work by the authors<sup>12</sup> shows, for example, that the recent improvement<sup>13</sup> on a model developed by Ghosh and Olson<sup>14</sup> for predicting  $M_s$  performs significantly worse than the original model if the appropriate database is not used

- (ii) such approaches rely on the availability of expensive thermodynamic calculation software, the costs of which are hardly justified for such an application alone
- (iii) the empirical component is not eliminated but displaced to lower levels of the model.

New empirical methods such as neural network (NN) analysis offer attractive advantages, being not only easily distributed and self-sufficient but also able to cover arbitrarily large ranges of data. As any other method, their domain of applicability is somewhat determined by the data available at the time the model is defined. However, a feature unique to the method employed in the present work is the ability of the model to accompany its predictions by an indication of their reliability.

### Predicting the $B_s$ temperature

In this section a brief description of neural network modelling is presented along with the thermodynamic theory for bainite transformation. The latter is necessary in order to understand the results and to be able to compare them with the empirical predictions obtained by means of the NN model developed in this paper.

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<sup>\*</sup>Corresponding author, email: cgm@cenim.csic.es



## The effect of silicon on the nanoprecipitation of cementite

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<sup>b</sup> MATERIALIA Group, Department of Physical Metallurgy, Centro Nacional de Investigaciones Metalúrgicas (CENIM-CSIC), Av. Gregorio del Amo 8, 28040 Madrid, Spain

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Available online 5 September 2013

### Abstract

The current work presents a comprehensive study that aims at understanding the role of silicon on  $\theta$  precipitation, as well as on the  $\epsilon \rightarrow \theta$  carbide transition in tempered martensite. Cementite nucleation was modelled under paraequilibrium conditions in order to ensure the presence of silicon in the carbide, where both thermodynamic and misfit strain energies were calculated to evaluate the overall free energy change. The growth stage was investigated using in situ synchrotron radiation; three alloys containing 1.4–2.3 wt% silicon contents have been studied. Silicon appears to play a significant role in carbide growth. It was observed throughout tempering that cementite precipitation was slower in the higher silicon content alloy. Literature reports that cementite growth is accompanied by silicon partitioning, where the silicon content inside the carbide decreases as tempering progresses. Therefore it appears that the limiting factor of the growth kinetics is the rate at which silicon is rejected from the carbide; the silicon piles up at the carbide–matrix interface, acting as a barrier for further growth.

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**Keywords:** Phase transformation; Synchrotron radiation; Carbides; Precipitation kinetics; Tempered martensite

### 1. Introduction

It is a well-established fact that silicon plays a retarding effect on the epsilon to cementite carbide transition in tempered martensitic steels [1,2]. This concept has attracted considerable industrial interest in the optimization of alloying in steels – see e.g. Nam et al. [3]. The retention of the  $\epsilon$  carbide phase leads to ultrahigh strength in steels, a property attributed to the presence of microstrains at the precipitate–matrix interface [4]. Consequently, near the  $\epsilon \rightarrow \theta$  transition a softening regime exists, where ductility is recovered at the expense of loss in strength. Being of considerable interest from both the academic and the industrial point of view, the role of silicon during tempering has been studied extensively over the past decades. This

project's initial interest was in the development of ultra-high-strength steels applications, where one aim was to understand the effect of silicon on carbide precipitation, which is the main focus of the current paper. By understanding the carbide transition at the microstructural level, alloy tailoring can be achieved, whereby improved mechanical properties allow for greater flexibility in designing structural components.

The general understanding has been that the  $\epsilon \rightarrow \theta$  transition, also known as the third stage of tempering, takes place in two steps: Stage IIIB, where the remaining C atoms within the matrix are taken up for cementite precipitation while  $\epsilon$ -carbide persists in the matrix. At Stage IIIB it has been thought that once the matrix becomes depleted, the  $\epsilon$ -carbide decomposes in order to assist in the further production of cementite. The kinetics has been related to the diffusion of carbon through low-carbon martensite in Stage IIIA, and to the mobility of substitutional elements or the self-diffusion of iron in Stage IIIB. The

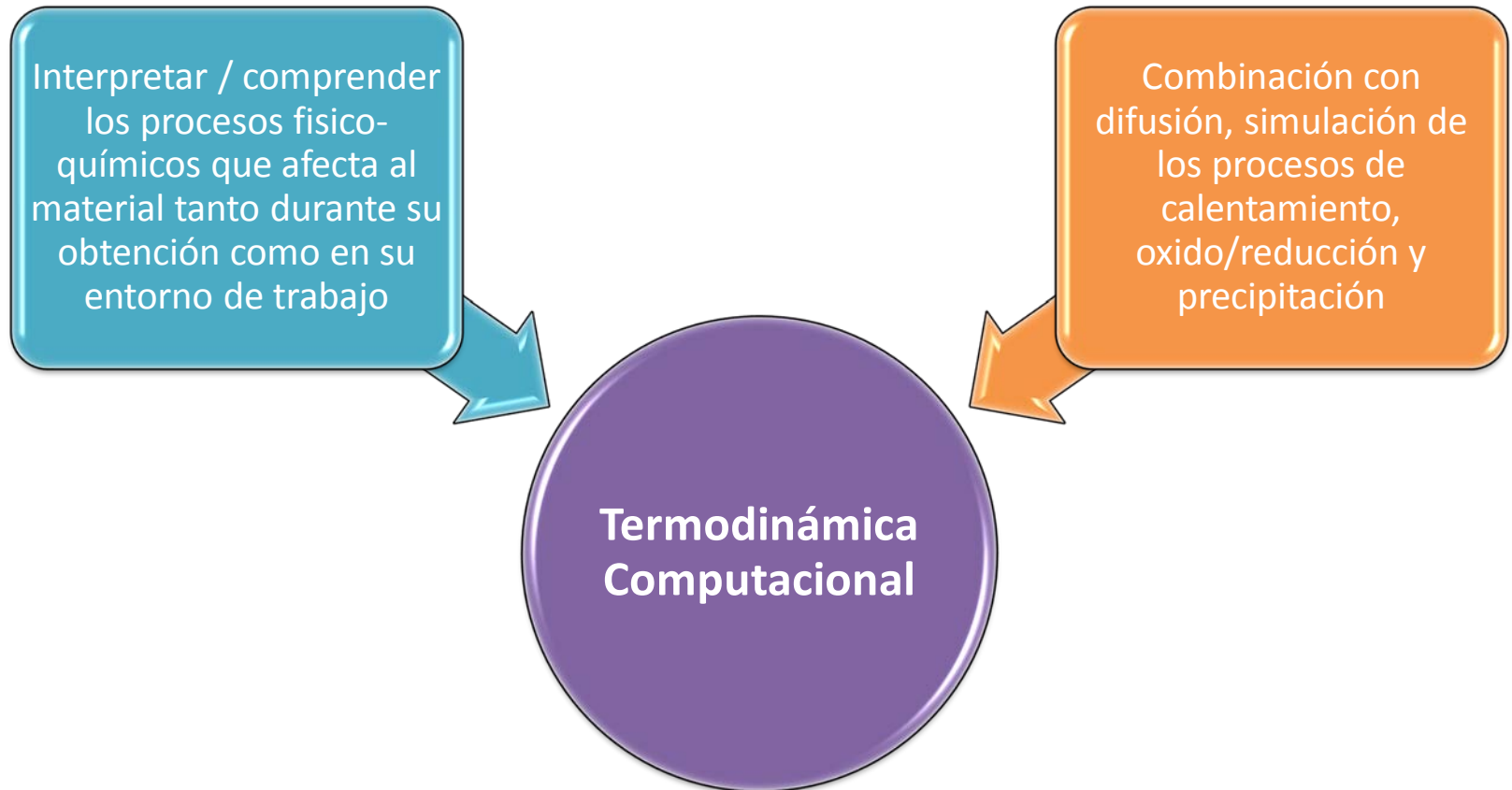
\* Corresponding author.  
E-mail address: [pej2@cam.ac.uk](mailto:pej2@cam.ac.uk) (P.E.J. Rivera-Díaz-del-Castillo).



## ¿Conclusión?

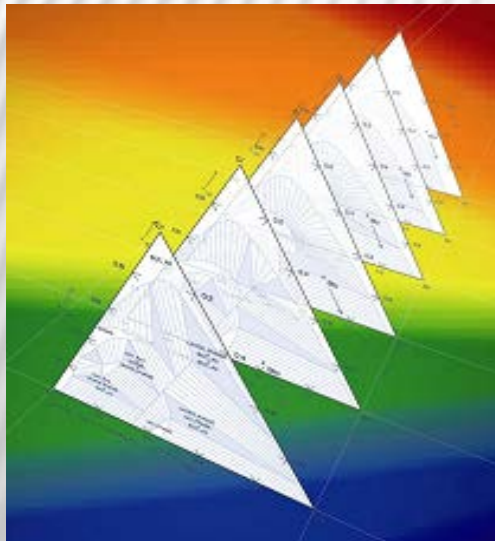
La metodología CALPHAD y los cálculos de primeros principios (Ab-initio) enfocados a determinar los parámetros necesarios para los cálculos de G en nuevos sistemas de aleación constituyen una poderosa herramienta de simulación en ciencia de materiales:

### **Termodinámica computacional**



# **T**aller Divulgativo en el CENIM

## **PARTE II: APLICACIÓN DE THERMOCALC EN LA TRANSFORMACIÓN PERLÍTICA.**



**M.M.Aranda**  
**C.Capdevila**



**Thermo-Calc Software**

[www.thermocalc.com](http://www.thermocalc.com)

**1.-INTRODUCCIÓN.**

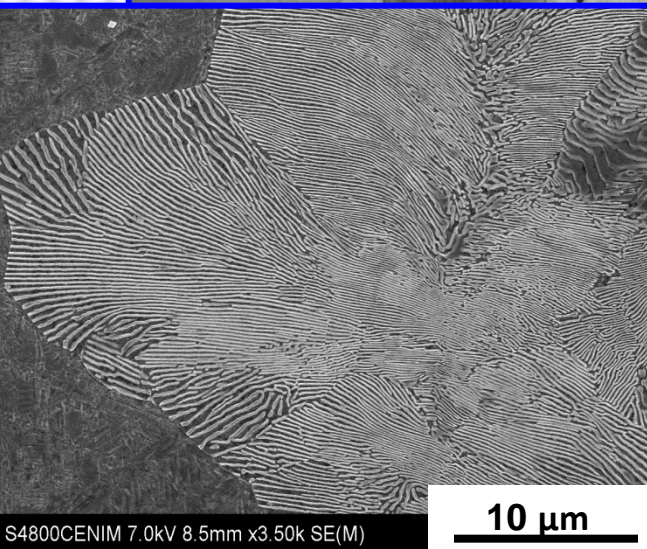
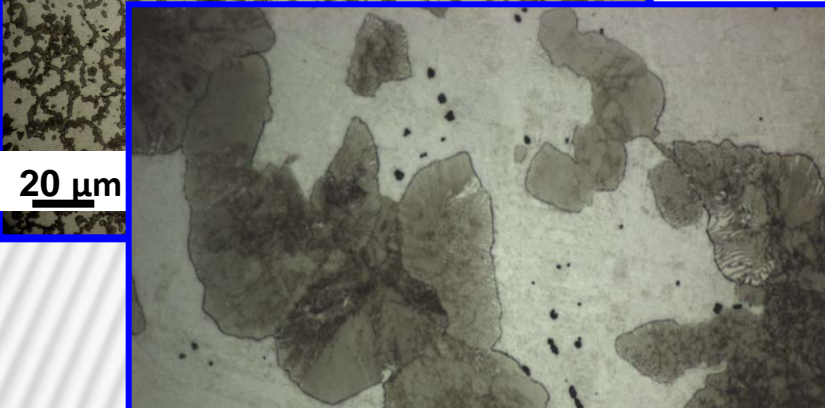
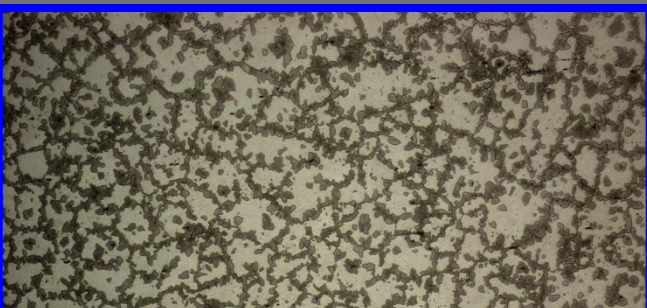
**2.-CÁLCULO DE DIAGRAMAS DE FASE:  
ISOPLETH E ISOTHERM.**

**3.-EXTRAPOLACIÓN DE HULTGREN.**

**4.-LÍNEAS DE PARTICIÓN-NO PARTICIÓN.**

**5.- COMPOSICIÓN DE LAS FASES.**

# 1.- INTRODUCCIÓN



## ESTUDIO DE LA TRANSFORMACIÓN PERLÍTICA EN UNA ALEACIÓN Fe-C-Mn.



Diseñar los tratamientos isotérmicos adecuados para el estudio de la transformación perlítica.



- DIAGRAMAS DE FASE.
- EXTRAPOLACIÓN DE HULGTREN.
- ELCP O ELSP: Localización de las regiones de Partición-no partición.
- COMOPOSICIONES INTERCARAS, COMPOSICIONES EQUILIBRIO.
- PERLITA CONSTANTE Y PERLITA DIVERGENTE



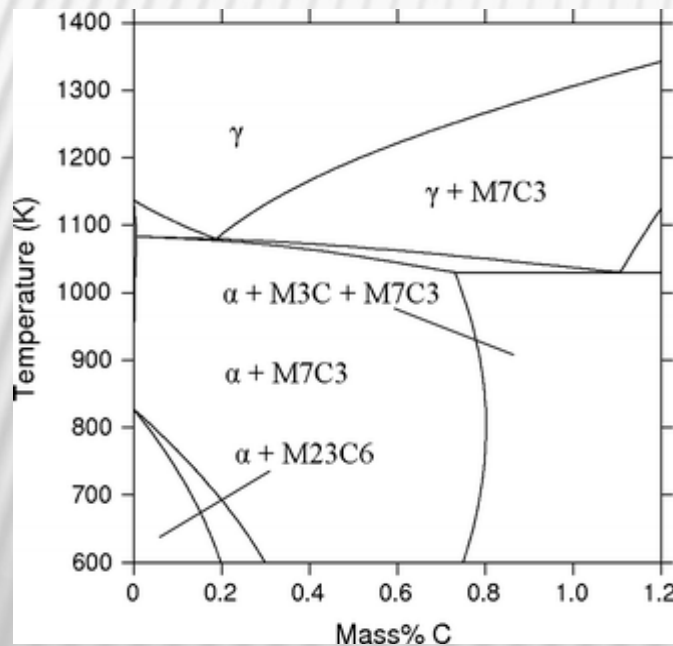
Thermo-Calc Software

[www.thermocalc.com](http://www.thermocalc.com)

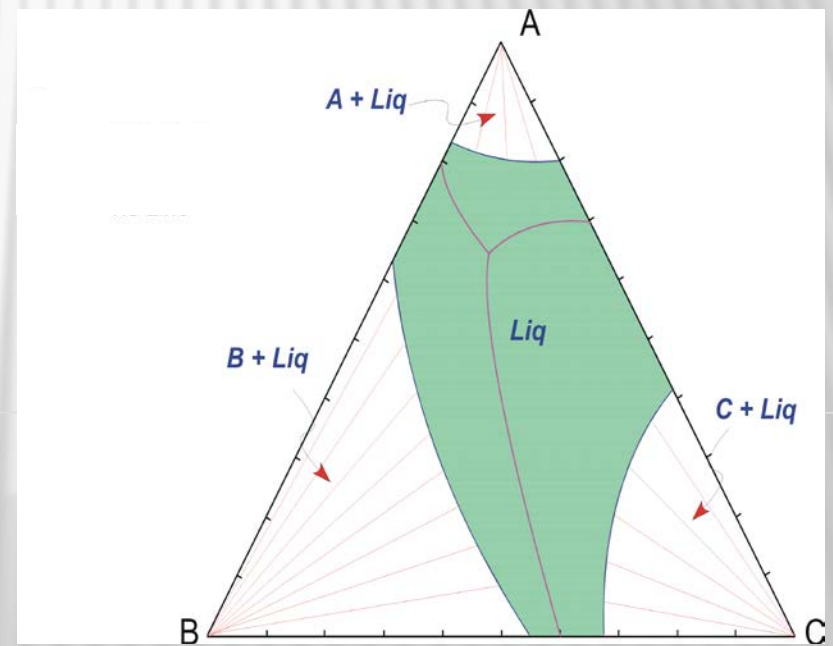


# CÁLCULO DE DIAGRAMAS DE FASE: ISOPLETH E ISOTHERM

ISOPLETH



ISOTHERM



## 2.- CÁLCULO DE DIAGRAMAS DE FASE: ISOPLETH E ISOTHERM

Seleccionar la base de datos

Definir la aleación

Posibles Fases

```
Thermo-Calc
File Tools Window Help
New Open Save Apply Auto Layout Snap to Grid Show Grid Switch to Graphical Mode
Console
Console 1
Thermo-Calc 3.0.1 (build 5993) on WinNT 32-bit wordlength
Compiler: Intel(R) Visual Fortran Composer Version 12.1.3.300 Build 20120130
License library version: 8.5.1.0017
Linked: Thu Jun 13 11:20:13 2013
Copyright (1993,2008) Foundation for Computational Thermodynamics,
Stockholm, Sweden
Only for use at 11204 National Center for Metallurgical Research (CENIM-CSIC)
Local contact Carlos Garcia-Mateo 101725

SYS:go d
THERMODYNAMIC DATABASE module
Current database: TCS Steels/Fe-Alloys Database v7.0

VA DEFINED
L12_FCC B2_BCC B2_VACANCY
HIGH_SIGMA DICTRA_FCC_A1 REJECTED
TDB_TCFE7: def-sys fe c mn
FE C MN
DEFINED
TDB_TCFE7: l-sys ph
GAS:G LIQUID:L BCC_A2
FCC_A1 HCP_A3 DIAMOND_FCC_A4
GRAPHITE CEMENTITE M23C6
M7C3 M5C2 KSI_CARBIDE
A1_KAPPA KAPPA FE4N_LP1
FECN_CHI LAVES_PHASE_C14 G_PHASE
```



## 2.- CÁLCULO DE DIAGRAMAS DE FASE: ISOPLETH E ISOTHERM

```
Thermo-Calc
File Tools Window Help
New Open Save Apply Auto Layout Snap to Grid Show Grid Switch to Graphical Mode
Console
Console 1
FECN_CHI LAVES_PHASE_C14 G_PHASE
TDB_TCFE7:rej ph *
GAS:G LIQUID:L BCC_A2
FCC_A1 HCP_A3 DIAMOND_FCC_A4
GRAPHITE CEMENTITE M23C6
M7C3 M5C2 KSI_CARBIDE
A1_KAPPA KAPPA FE4N_LP1
FECN_CHI LAVES_PHASE_C14 G_PHASE
REJECTED
TDB_TCFE7:restore ph fcc bcc cem
FCC_A1 BCC_A2 CEMENTITE
RESTORED
TDB_TCFE7:get
REINITIATING GES5 .....
ELEMENTS .....
SPECIES .....
PHASES .....
PARAMETERS ...
FUNCTIONS ....

List of references for assessed data

'A. Dinsdale, SGTE Data for Pure Elements, Calphad, 15 (1991), 317-425'
'P. Franke, estimated parameter within SGTE, 2007; Fe-C, Ni-C, Mo-C, C-Mn'
'P. Gustafson, Scan. J. Metall., 14 (1985), 259-267; TRITA 0237 (1984); C
-FE'
```

Seleccionar las  
posibles fases  
presentes para la  
aleación de interés

## 2.- CÁLCULO DE DIAGRAMAS DE FASE: ISOPLETH E ISOTHERM

Condiciones: P,T,  
composiciones....

```
TDB_TCFE7 go p-3
```

```
POLY version 3.32
```

```
POLY_3 s-c p=1e5 n=1 t=1200 x(c)=0.03 x(mn)=0.1
```

```
POLY_3:l-c
```

```
P=1E5, N=1, T=1200, X(C)=3E-2, X(MN)=0.1
```

```
DEGREES OF FREEDOM 0
```

```
POLY_3:c-e
```

```
Global equilibrium calculation turned off, you can turn it on with  
ADVANCED_OPTIONS GLOBAL_MINIMIZATION Y,,,,,,,,
```

```
16 ITS, CPU TIME USED 0 SECONDS
```

```
POLY_3:s-a-v 1 x(c)
```

```
Min value /0/:
```

```
Max value /1/:
```

```
Increment /.025/:
```

```
POLY_3:s-a-v 2 t
```

```
Min value /0/:400
```

```
Max value /1/:1200
```

```
Increment /20/:
```

```
POLY_3:save
```

ISOPLETH

## 2.- CÁLCULO DE DIAGRAMAS DE FASE: ISOPLETH E ISOTHERM

```
POLY_3:map
```

```
Version S mapping is selected
```

```
POLY_3:post
```

```
POLY-3 POSTPROCESSOR VERSION 3.0
```

```
Setting automatic diagram
```

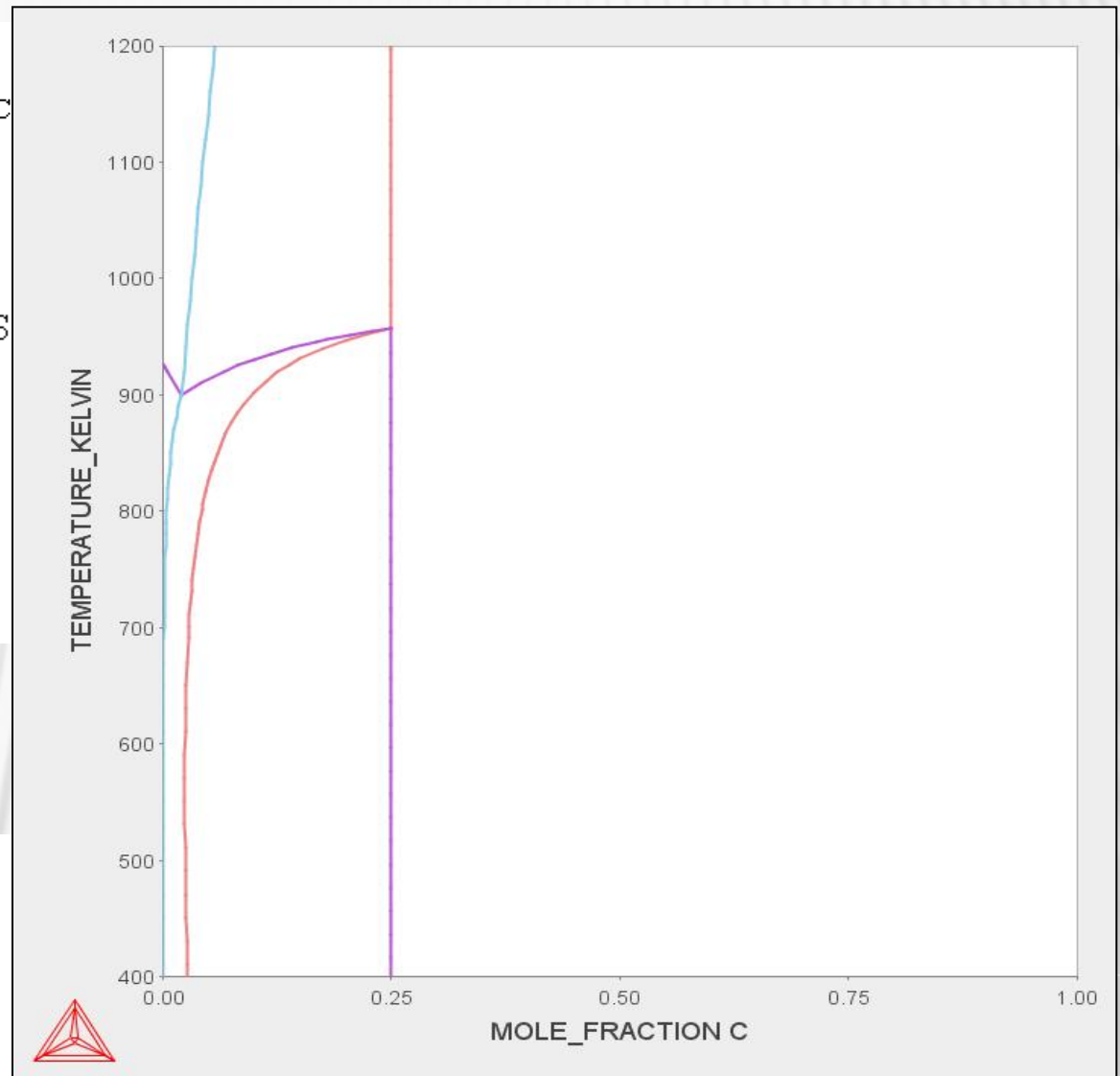
```
POST:plot
```

```
POST:s-s-s x n 0 0.1
```

```
POST:s-s-s y n 600 1000
```

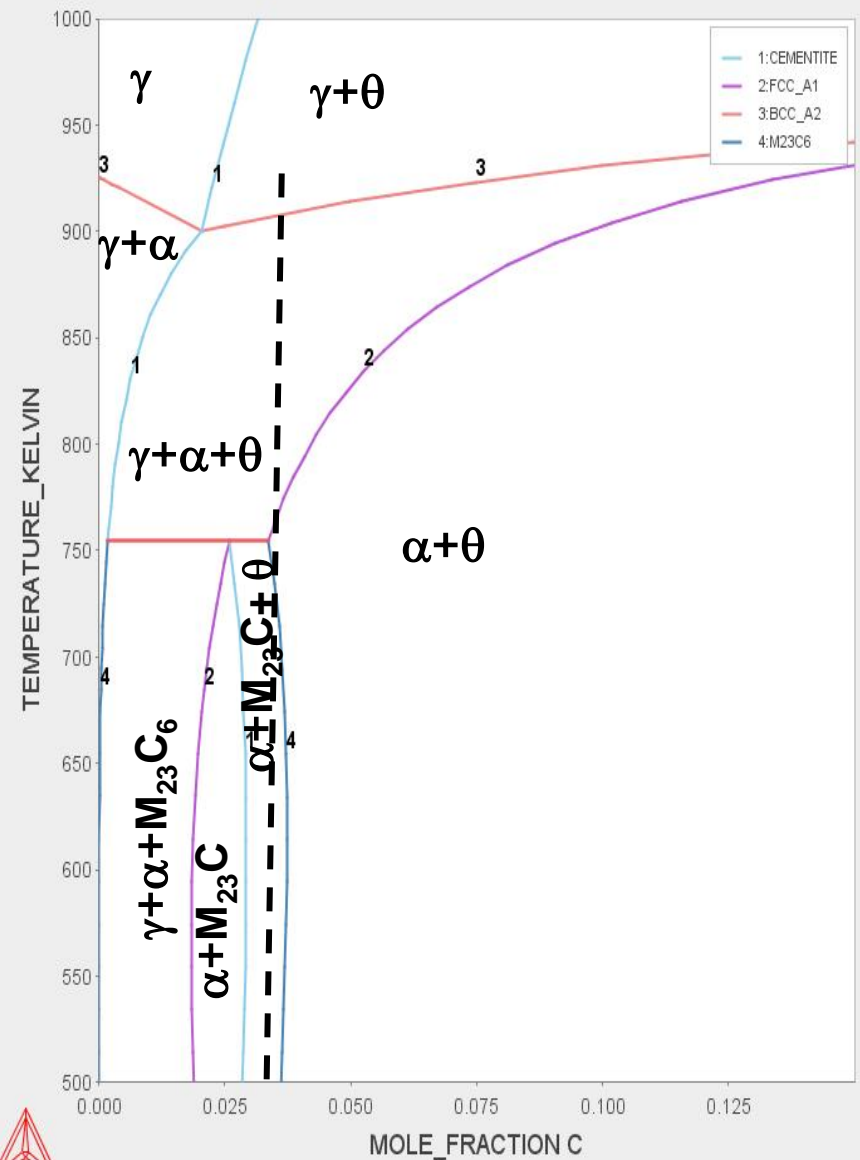
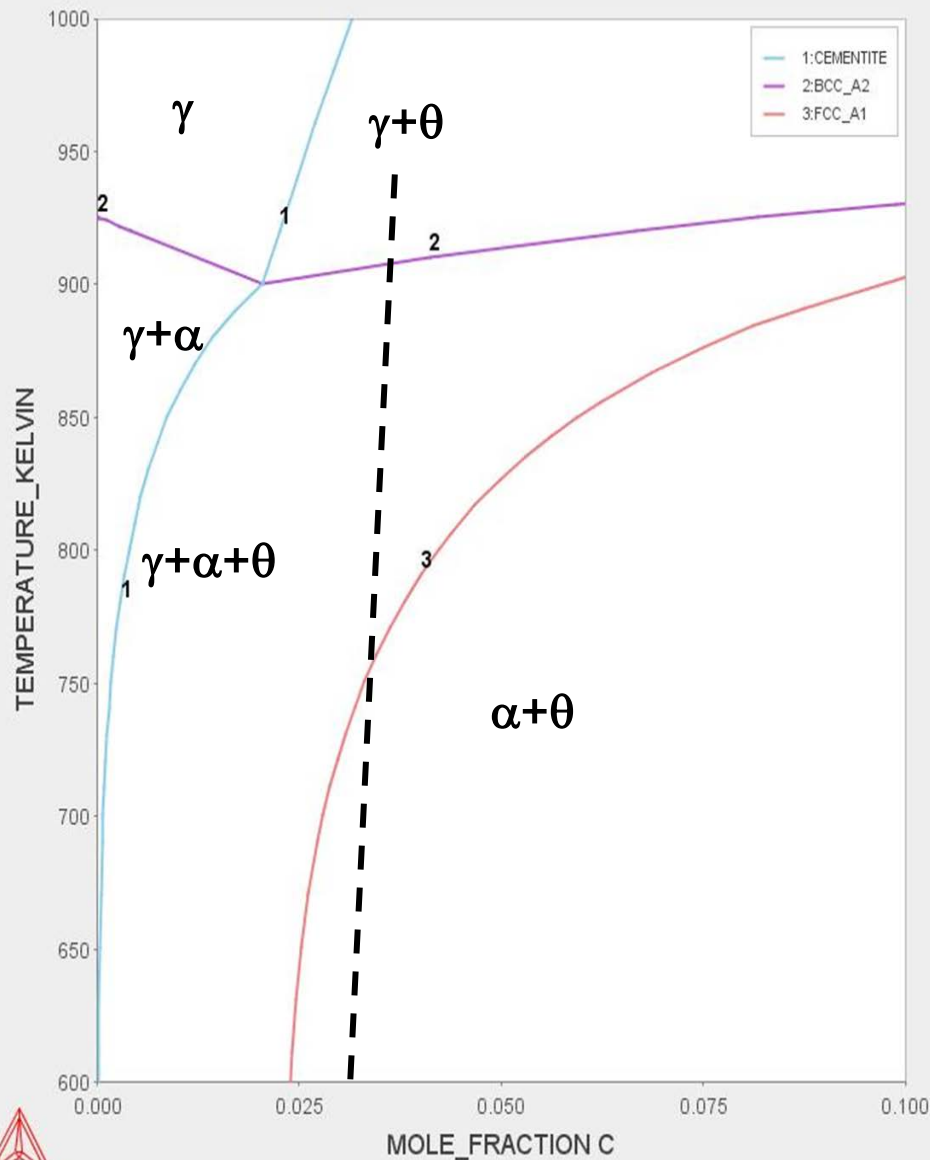
```
POST:s-lab e
```

```
POST:plot
```



# 2.- CÁLCULO DE DIAGRAMAS DE FASE: ISOPLETH E ISOTHERM

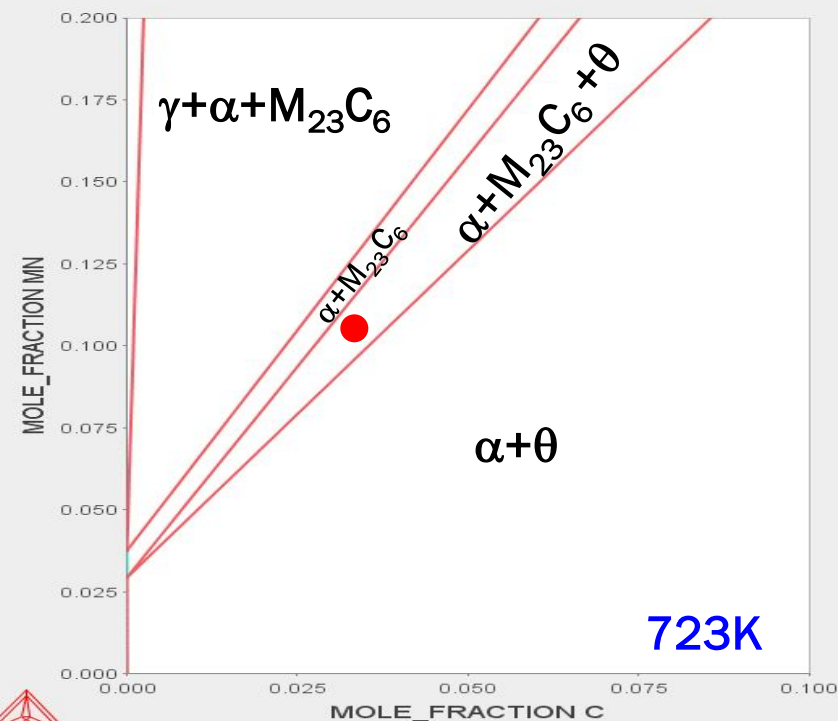
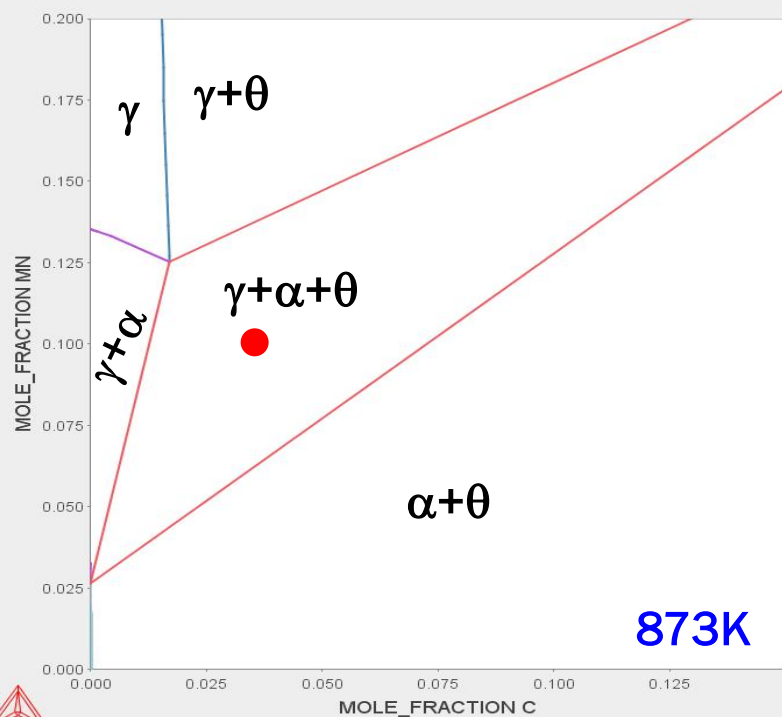
## SELECCIÓN DE TEMPERATURA PARA LOS TRATAMIENTOS ISOTÉRMICOS



## 2.- CÁLCULO DE DIAGRAMAS DE FASE: ISOPLETH E ISOTHERM

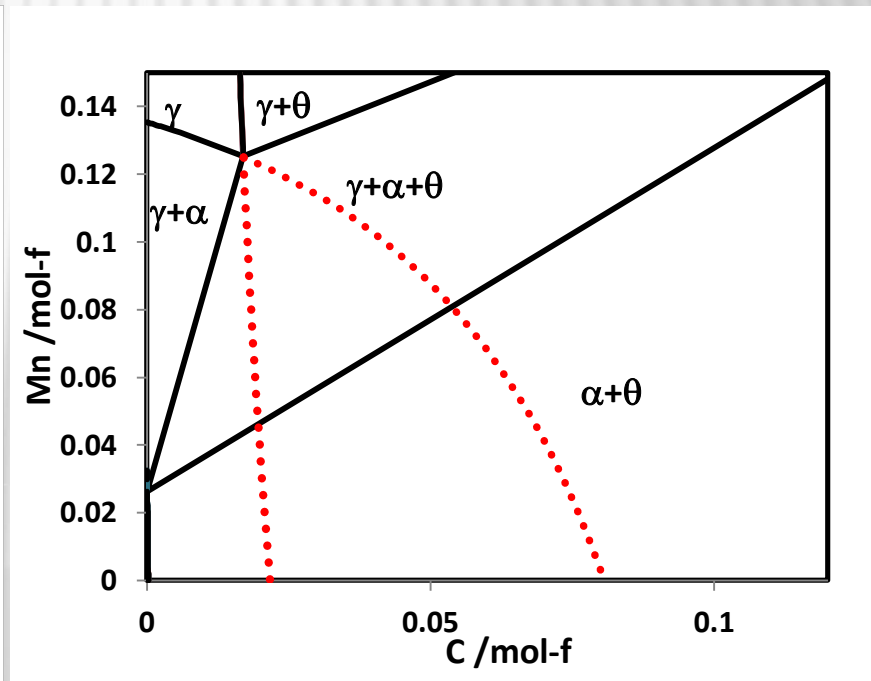
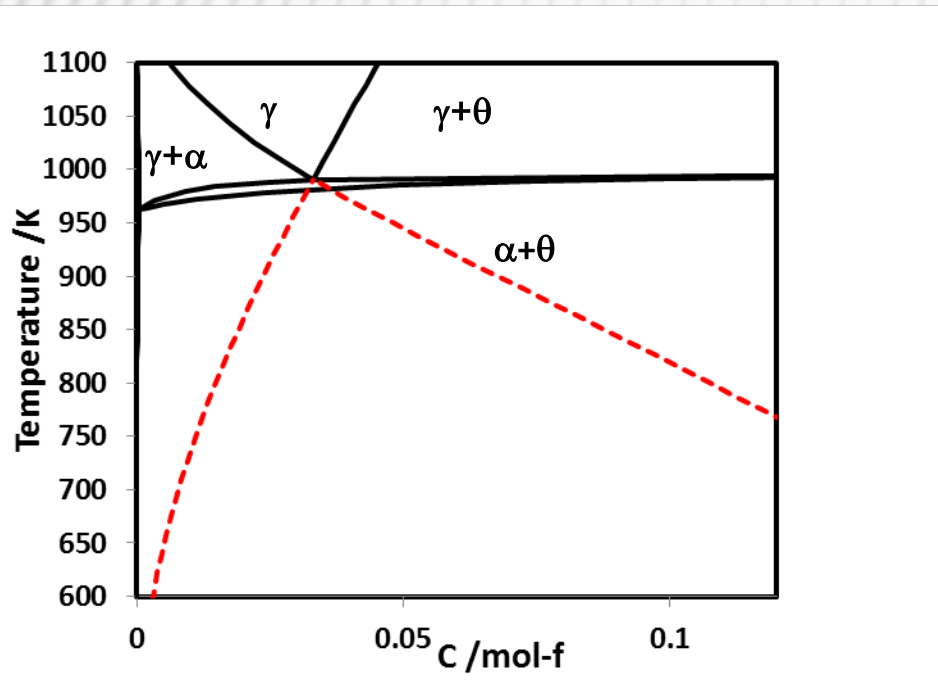
```
POLY version 3.32
POLY_3:s-c t=873 n=1 p=1e5 x(c)=0.03 x(mn)=0.1
POLY_3:l-c
T=873, N=1, P=1E5, X(C)=3E-2, X(MN)=0.1
DEGREES OF FREEDOM 0
POLY_3:c-e
Global equilibrium calculation turned off, you can turn it on with
ADVANCED_OPTIONS GLOBAL_MINIMIZATION Y,,,,,,,,
19 ITS, CPU TIME USED 0 SECONDS
POLY_3:s-a-v 1 x(c) 0 1
Increment /.025/:
POLY_3:s-a-v 2 x(mn) 0 1
Increment /.025/:
POLY_3:map
```

} ISOTHERM

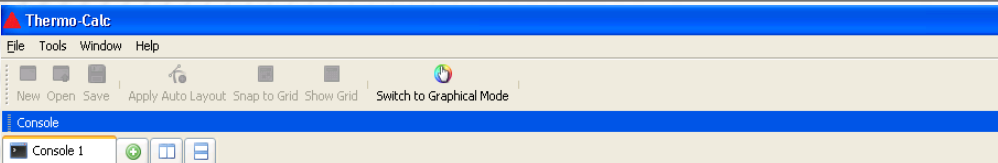


# EXTRAPOLACIÓN DE HULTGREN: EXTRAPOLACIÓN DE LAS LÍNEAS

$\gamma/\gamma+\alpha$   
 $\gamma/\gamma+\theta$



### 3.- EXTRAPOLACIÓN DE LAS LÍNEAS $\gamma/\gamma+\alpha$ $\gamma/\gamma+\theta$



**SYS:go d**

THERMODYNAMIC DATABASE module

Current database: TCS Steels/Fe-Alloys Database v7.0

VA DEFINED

L12\_FCC B2\_BCC B2\_VACANCY

HIGH\_SIGMA DICTRA\_FCC\_A1 REJECTED

**TDB\_TCFE7:def-sys fe c mn**

FE C MN

DEFINED

**TDB\_TCFE7:rej ph \***

**TDB\_TCFE7:restore ph fcc bcc**

**TDB\_TCFE7:get**

**TDB\_TCFE7:go p-3**

POLY version 3.32

**POLY\_3:s-c t=873 n=1 p=1e5 x(mn)=0.1 x(c)=0.03**

**POLY\_3:l-c**

T=873, N=1, P=1E5, X(MN)=1E-1, X(C)=0.03

DEGREES OF FREEDOM 0

**POLY\_3:c-e**

**POLY\_3:s-a-v 1 x(c) 0 1**

Increment /.025/:

**POLY\_3:s-a-v 2 x(mn) 0 1**

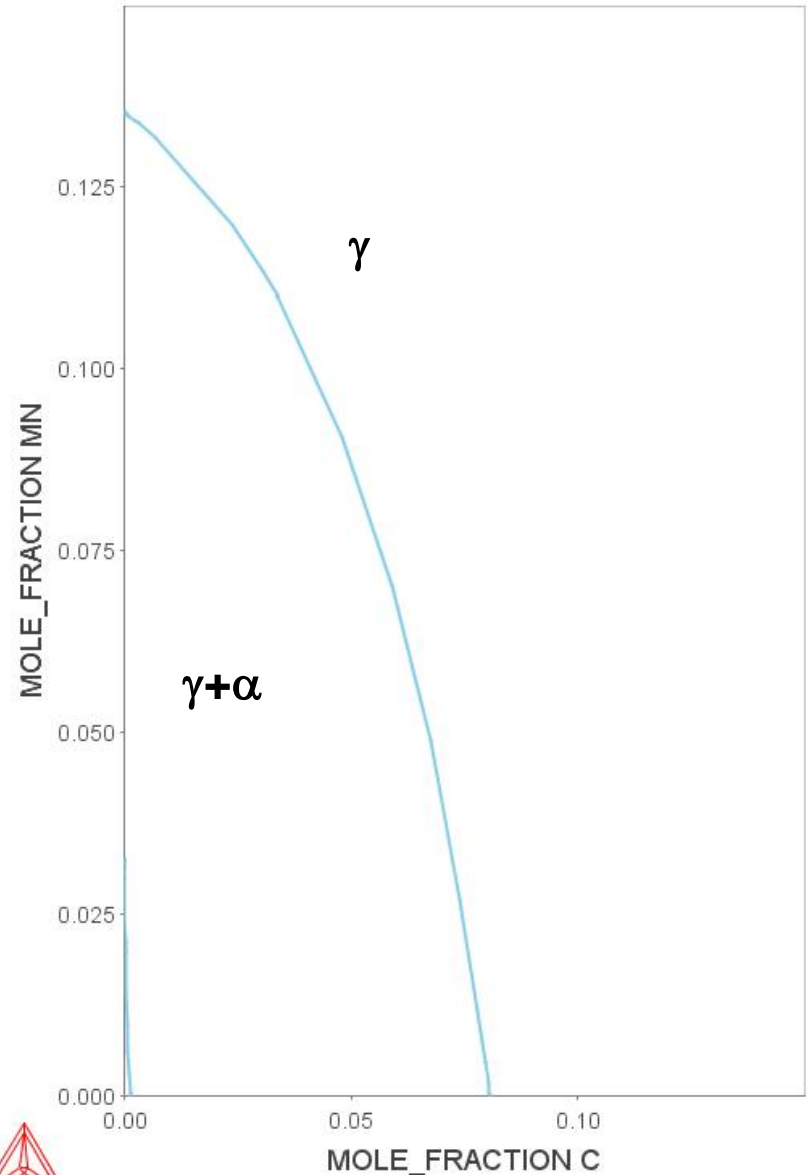
**POLY\_3:map**

**POLY\_3:post**

**POST:s-s-s x n 0 0.15**

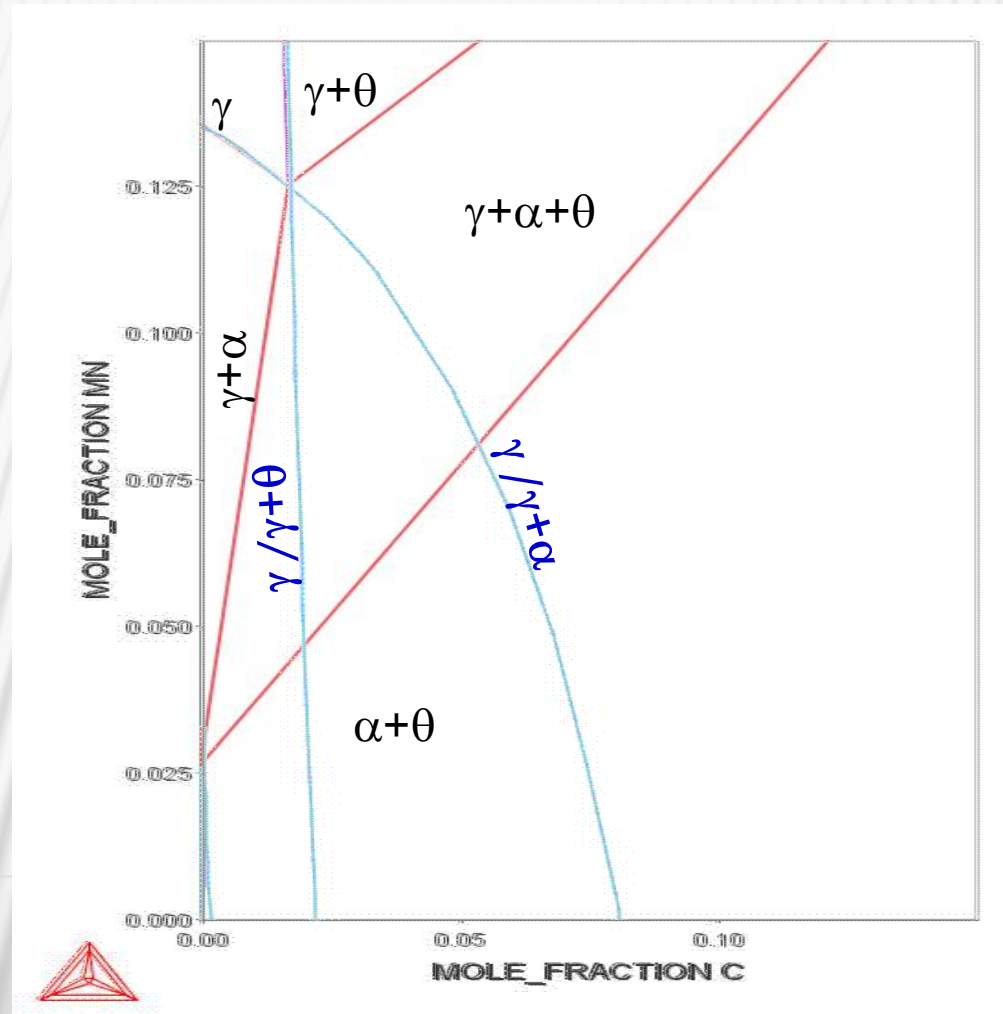
**POST:s-s-s y n 0 0.15**

**POST:pl**



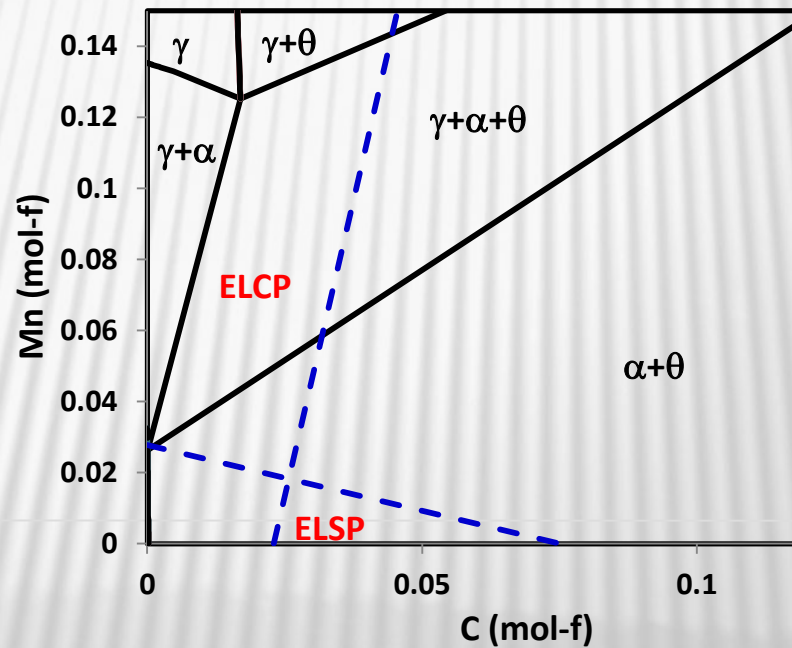


Superposición de las líneas  $\gamma/\gamma+\alpha$  y  $\gamma/\gamma+\theta$  en el diagrama de fases

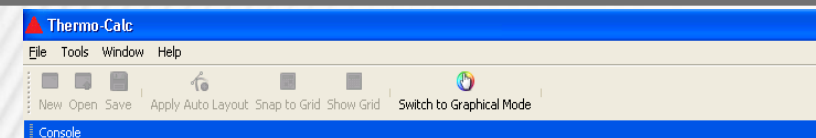




# LÍNEAS DE PARTICIÓN-NO PARTICIÓN



# 4.- LÍNEAS DE PARTICIÓN-NO PARTICIÓN



**SYS:go d**

**@SÓLO TENDREMOS EN CUENTA LA FASE AUSTENITA y FERRITA!, todas las demás fases las suspenderemos.**

HIGH\_SIGMA DICTRA\_FCC\_A1 REJECTED

**TDB\_TCFE7:def-sys fe c mn**

FE C MN

DEFINED

**TDB\_TCFE7:rej ph \***

**TDB\_TCFE7:restore ph fcc bcc**

**TDB\_TCFE7:get**

**TDB\_TCFE7:go p-3**

POLY version 3.32

**POLY\_3:s-c t=873 n=1 p=1e5 x(mn)=0.1 x(c)=0.03**

**POLY\_3:l-c**

T=873, N=1, P=1E5, X(MN)=1E-1, ACR(C)=0.055

DEGREES OF FREEDOM 0

**POLY\_3:c-e**

**POLY\_3:s-a-v 1 x(c) 0 1**

Increment /.025/:

**POLY\_3:s-a-v 2 x(mn) 0 1**

**POLY\_3:map**

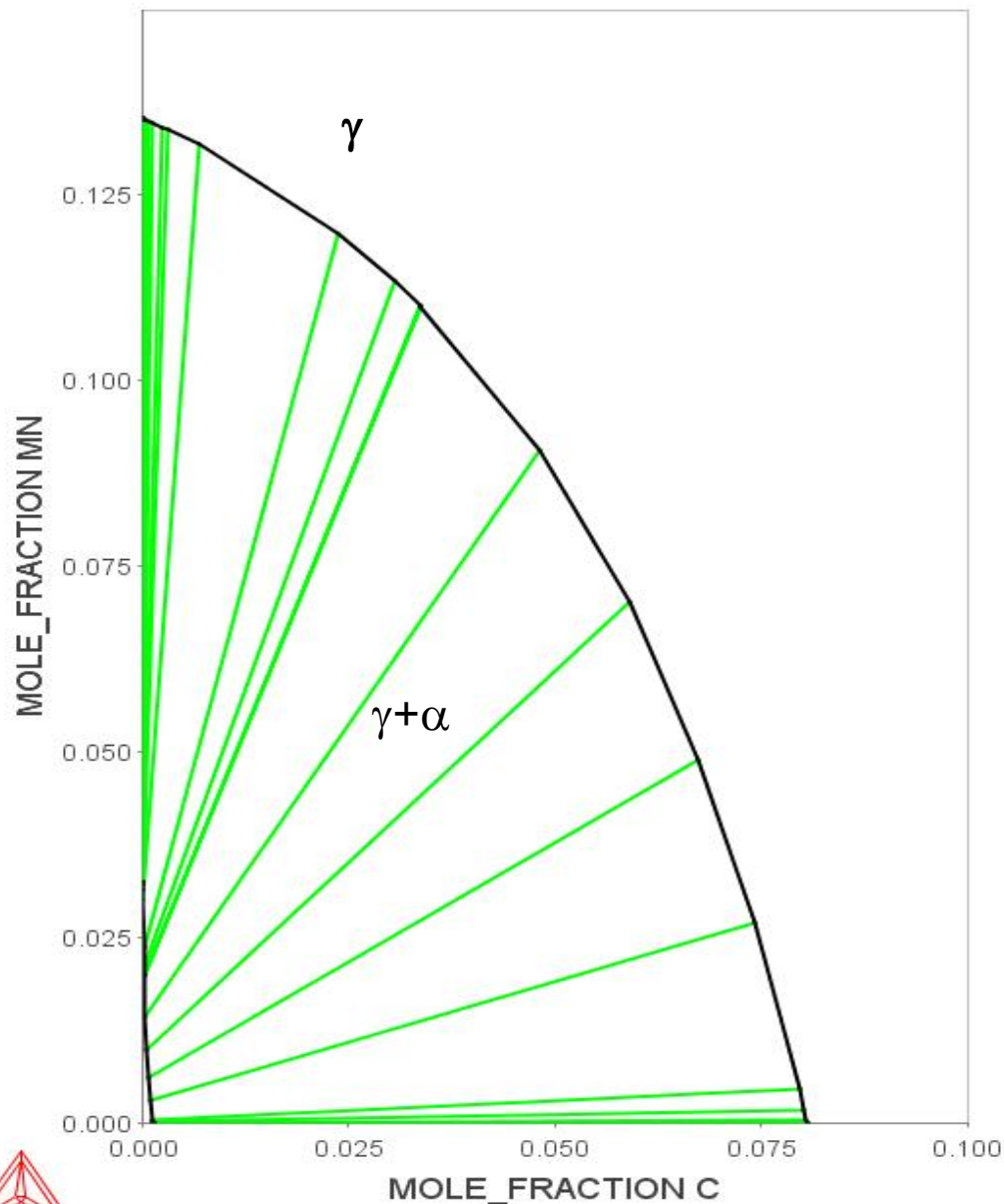
**POLY\_3:post**

**POLY\_3:s-t-s 1**

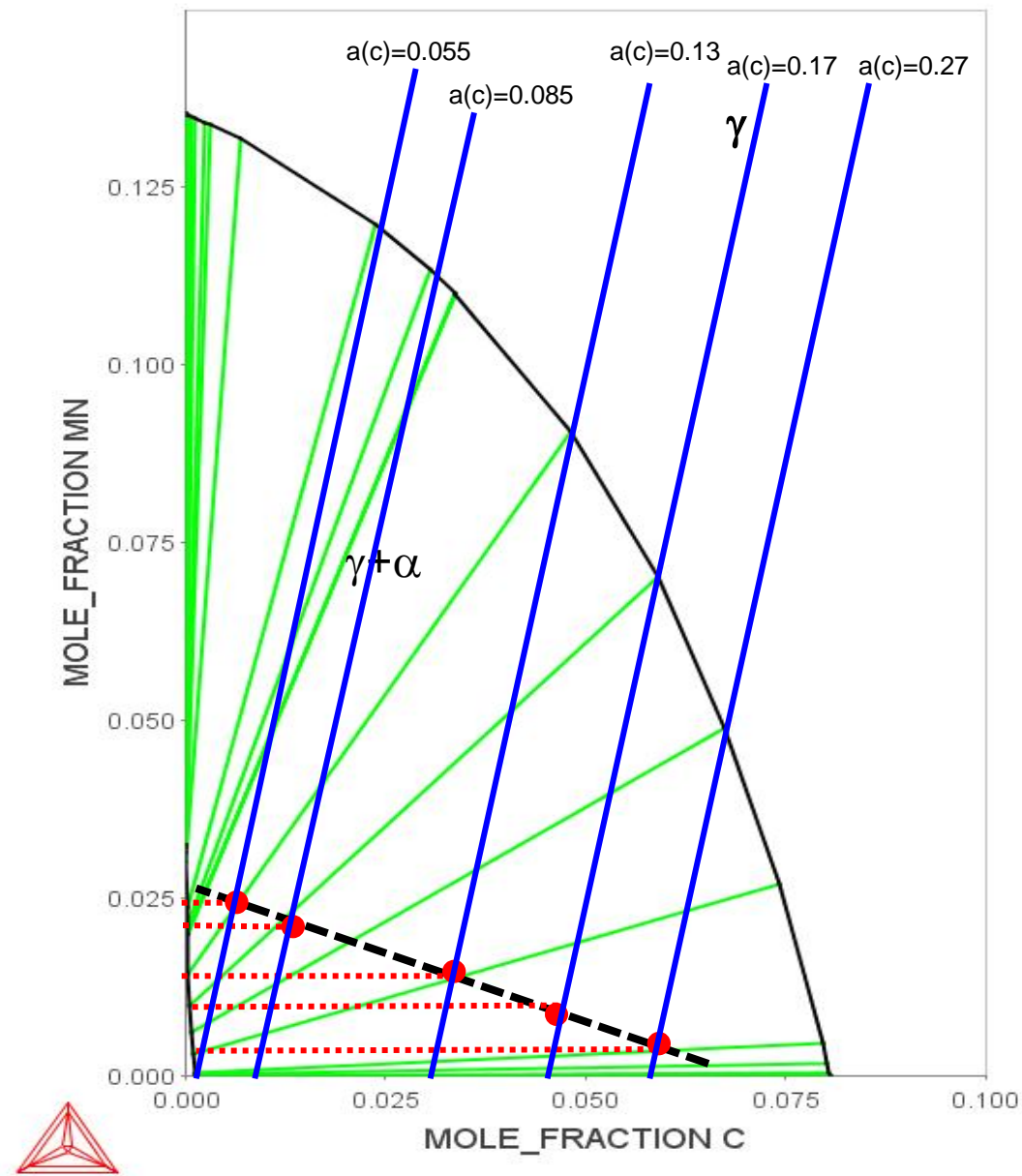
**POST:s-s-s x n 0 0.1**

**POST:s-s-s y n 0.15**

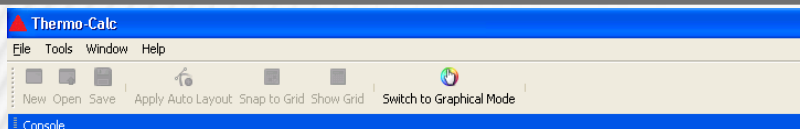
**POST:pl**



# 4.- LÍNEAS DE PARTICIÓN-NO PARTICIÓN



# 4.- LÍNEAS DE PARTICIÓN-NO PARTICIÓN



**SYS:go d**

**@Para calcular las líneas de isoactividad  
SÓLO TENDREMOS EN CUENTA LA FASE AUSTENITA!,  
todas las demás fases las suspenderemos.**

**TDB\_TCFE7: def-sys fe c mn**

FE C MN

DEFINED

**TDB\_TCFE7: rej ph \***

**TDB\_TCFE7: restore ph fcc**

**TDB\_TCFE7: get**

**TDB\_TCFE7: go p-3**

POLY version 3.32

**POLY\_3: s-c t=873 n=1 p=1e5 x(mn)=0.1 acr(c)=0.055**

**POLY\_3: l-c**

T=873, N=1, P=1E5, X(MN)=1E-1, ACR(C)=0.055

DEGREES OF FREEDOM 0

**POLY\_3: c-e**

**POLY\_3: s-a-v 1 x(mn) 0 1**

Increment /.025/:

**POLY\_3: step**

**POLY\_3: post**

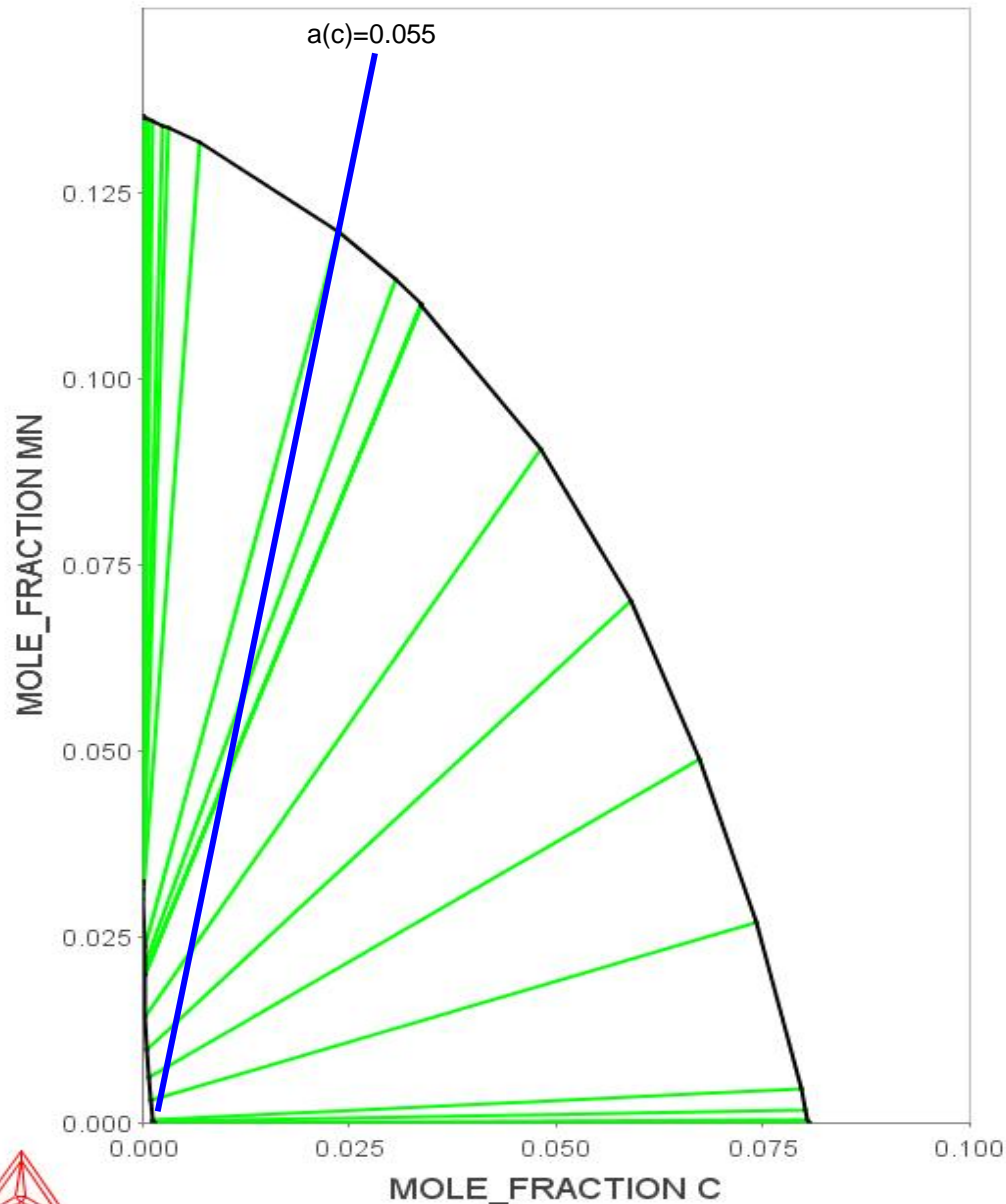
**POLY\_3: s-d-a x x(c)**

**POLY\_3: s-d-a y x(mn)**

**POST: s-s-s x n 0 0.1**

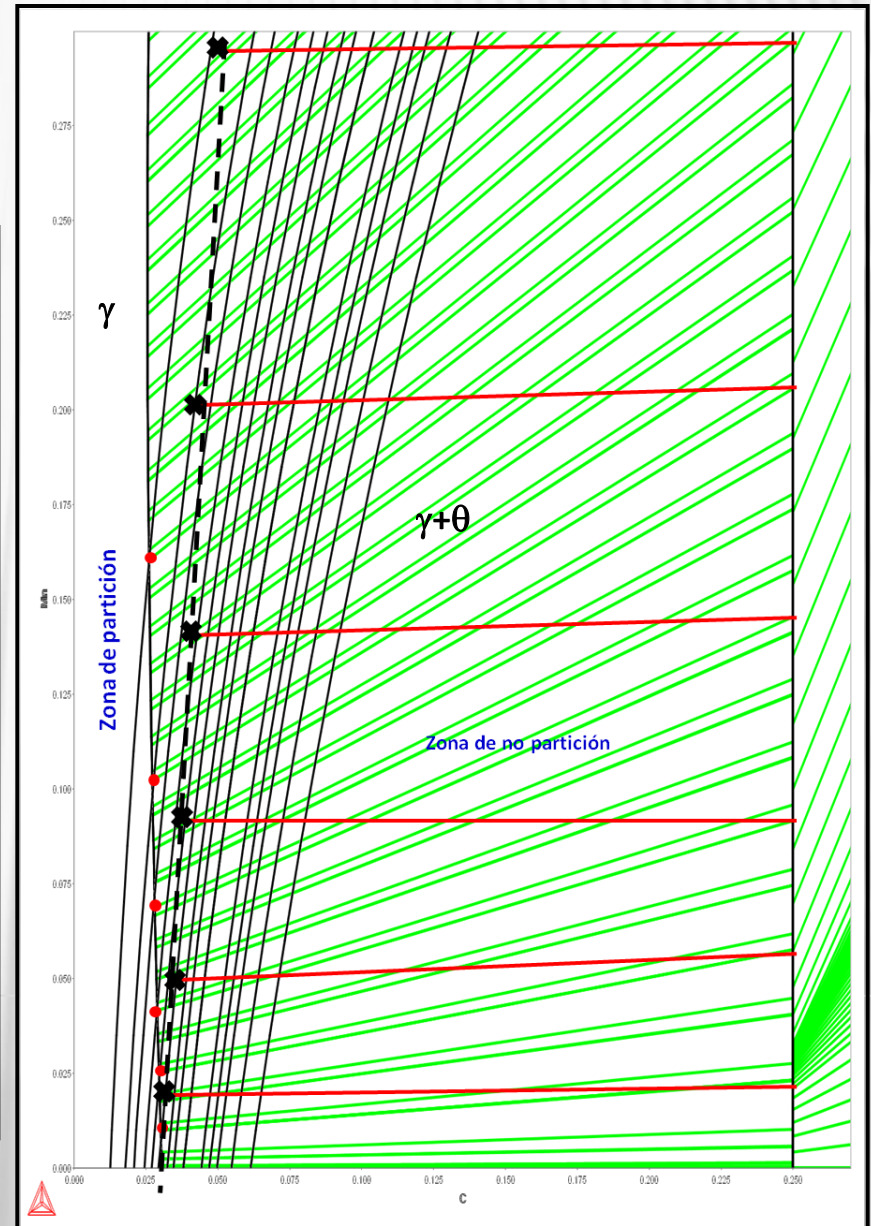
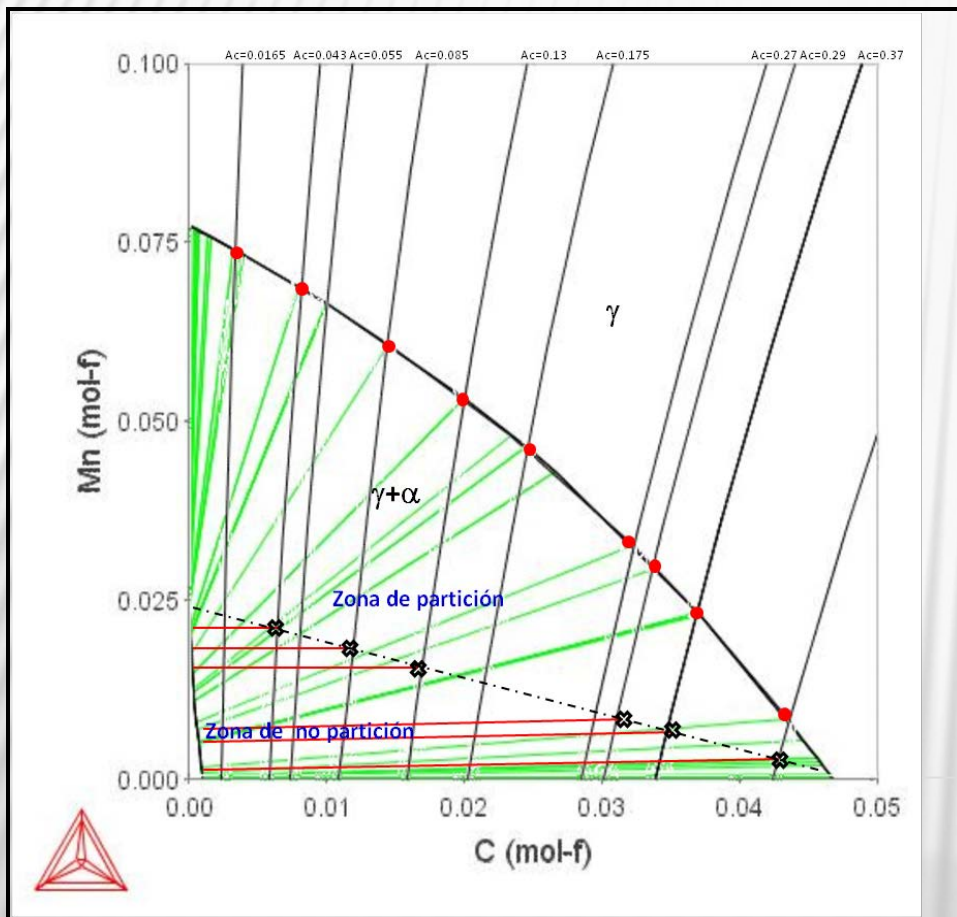
**POST: s-s-s y n 0.15**

**POST: pl**



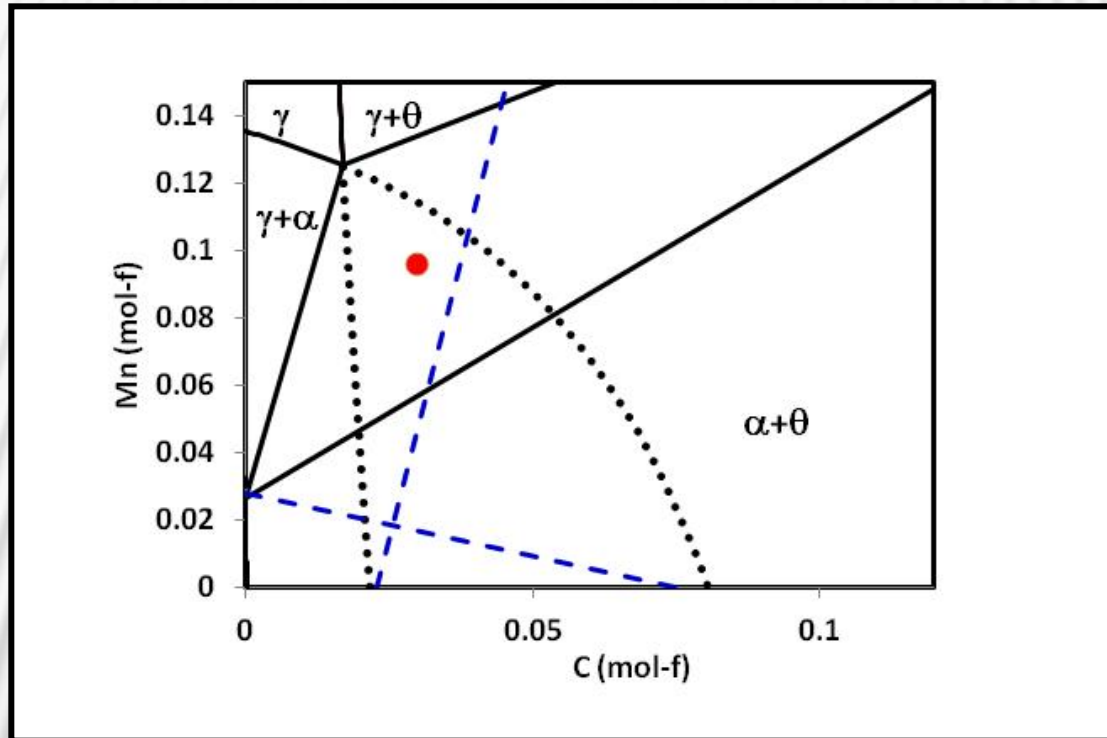


# 4.- LÍNEAS DE PARTICIÓN-NO PARTICIÓN



## 4.- LÍNEAS DE PARTICIÓN-NO PARTICIÓN

**Crecimiento de perlita con partición (ELCP) y sin partición (ELSP) de Mn.**



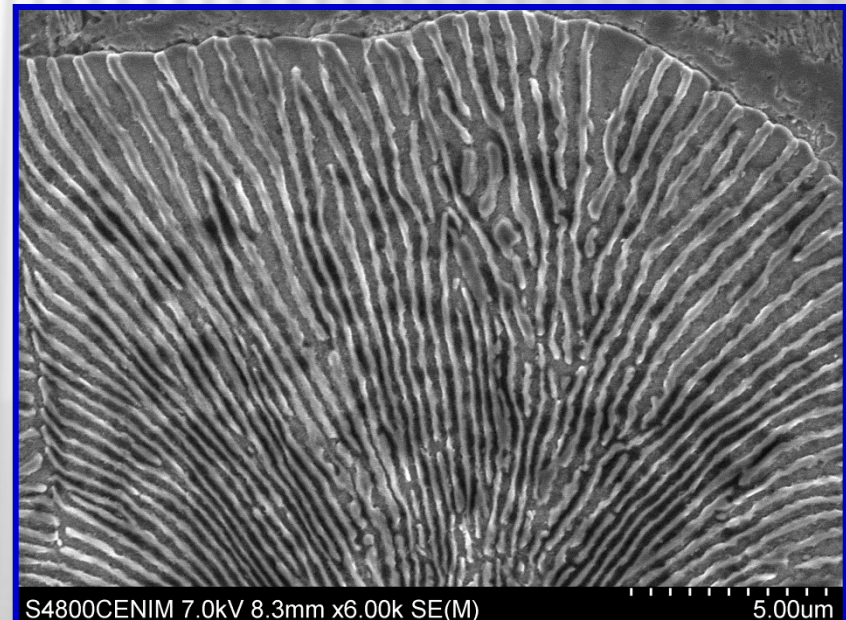
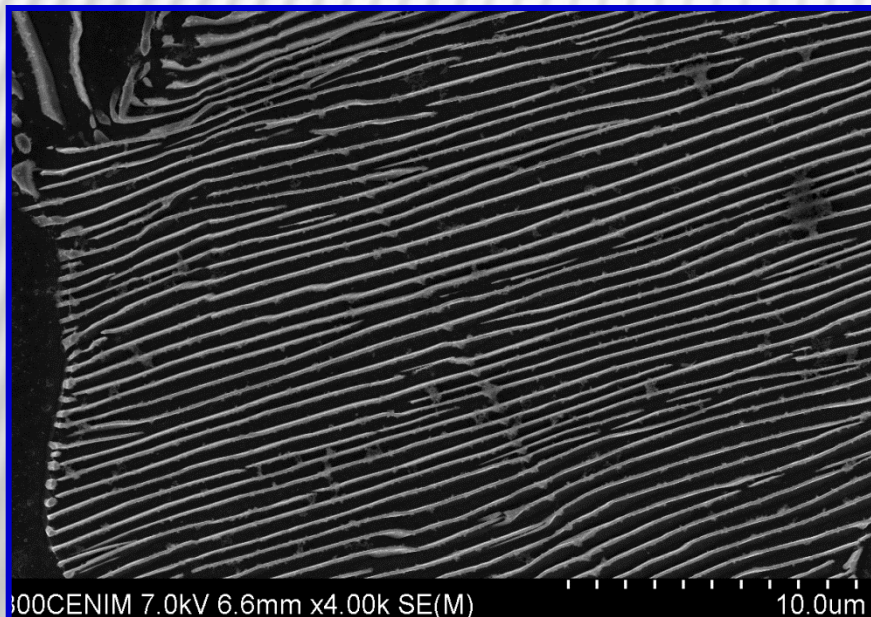
# COMPOSICIÓN DE LAS INTERCARAS

$\gamma/\gamma+\alpha$

$\gamma/\gamma+\theta$

## EQUILIBRIO LOCAL Y EQUILIBRIO

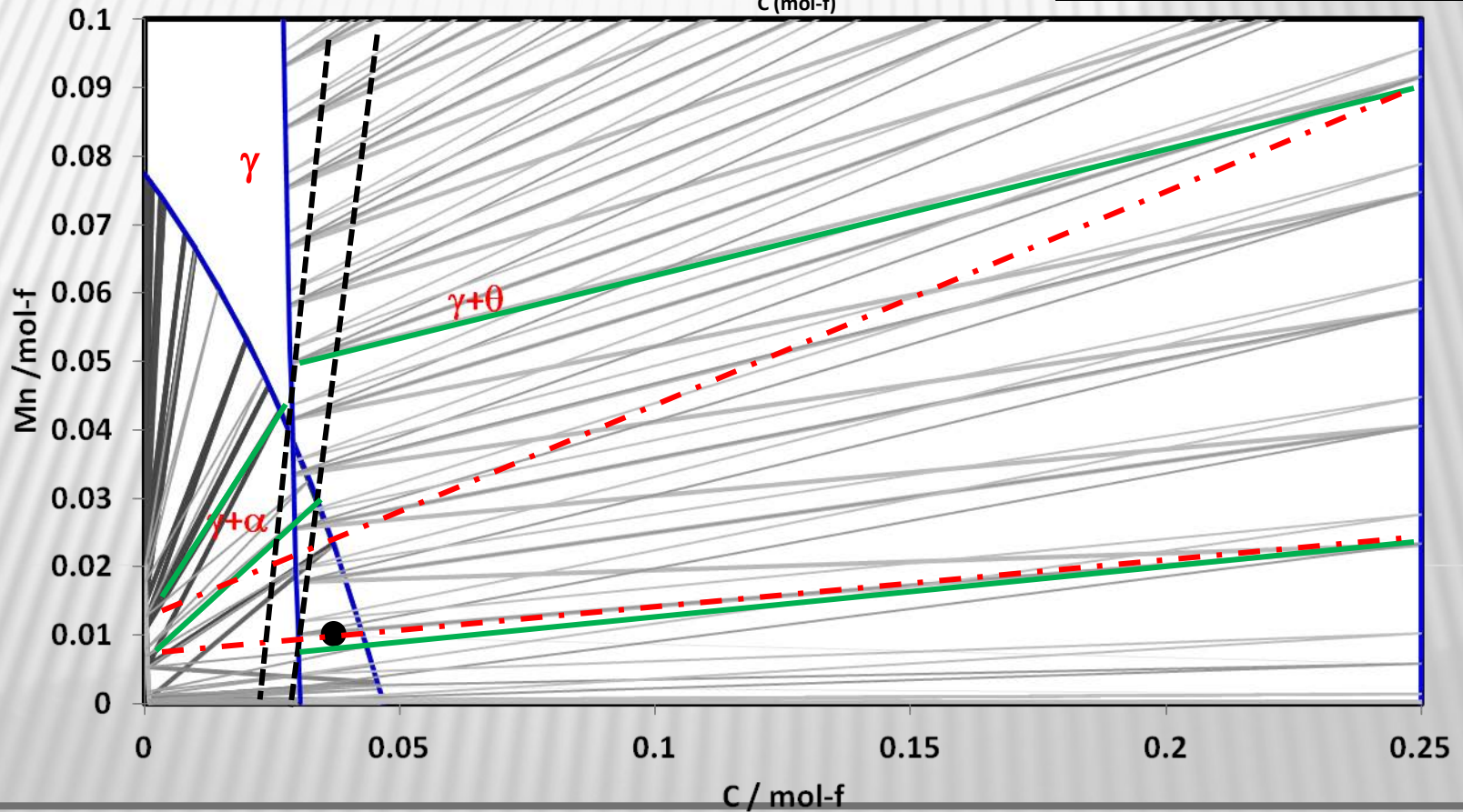
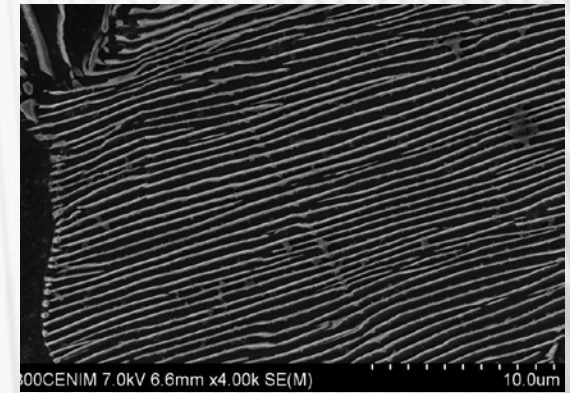
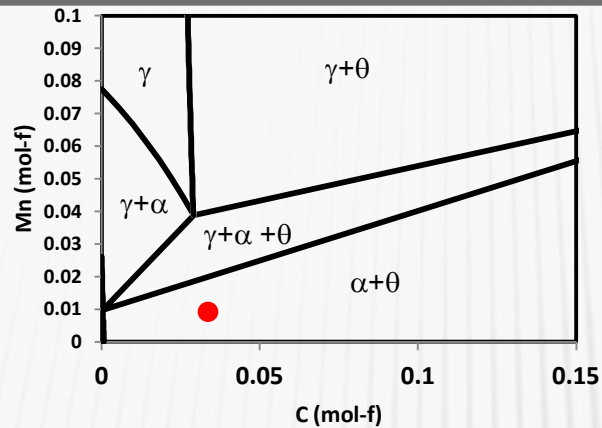
- PERLITA CONSTANTE
- PERLITA DIVERGENTE





# 5.- COMPOSICIÓN DE LAS FASES

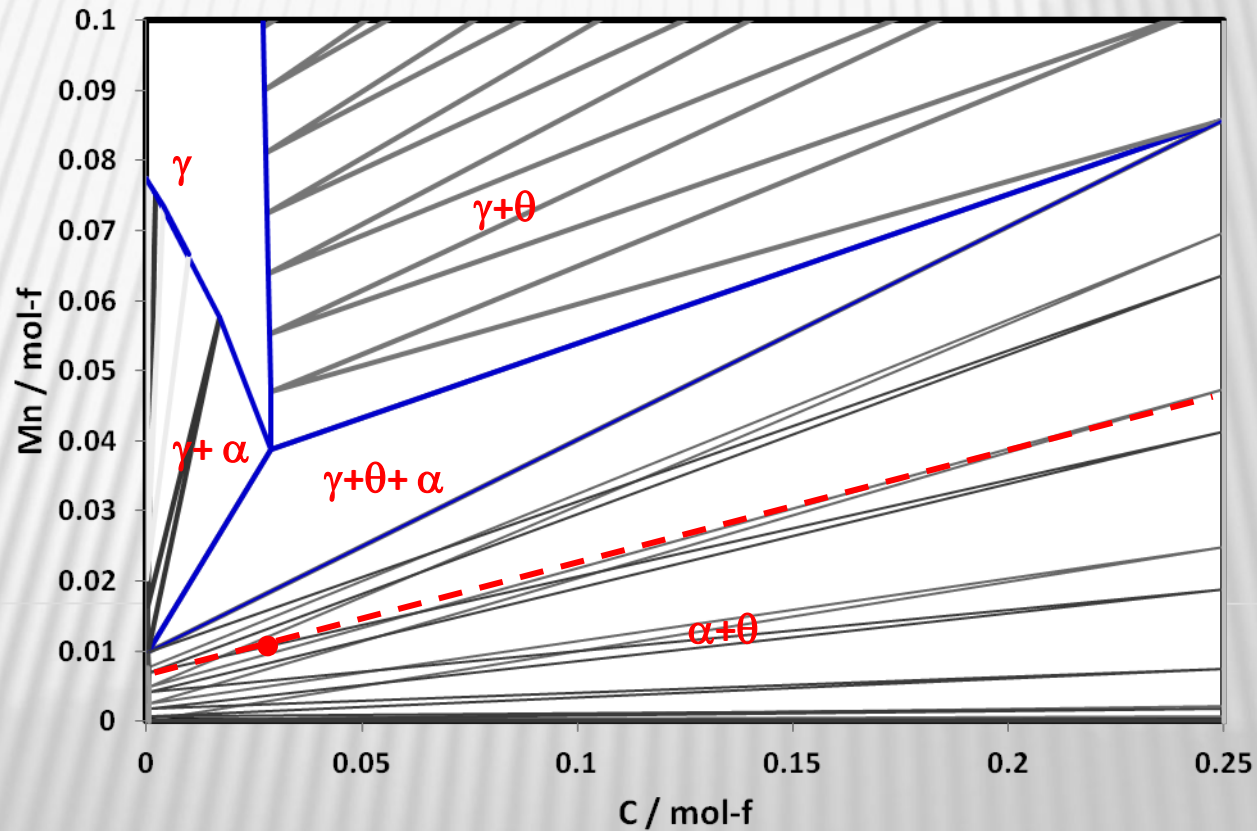
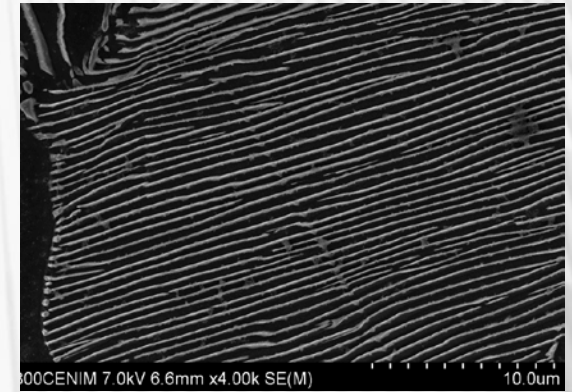
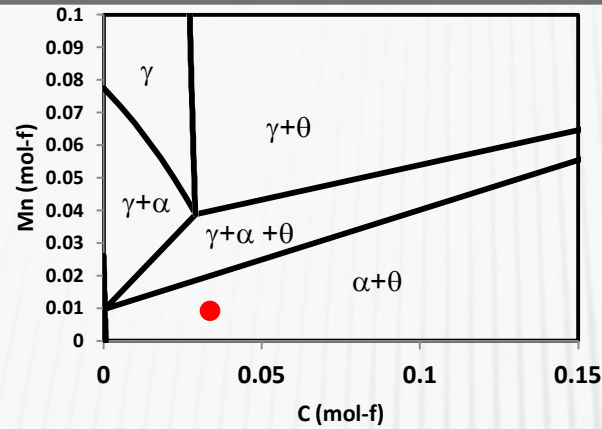
## EL PERLITA CONSTANTE





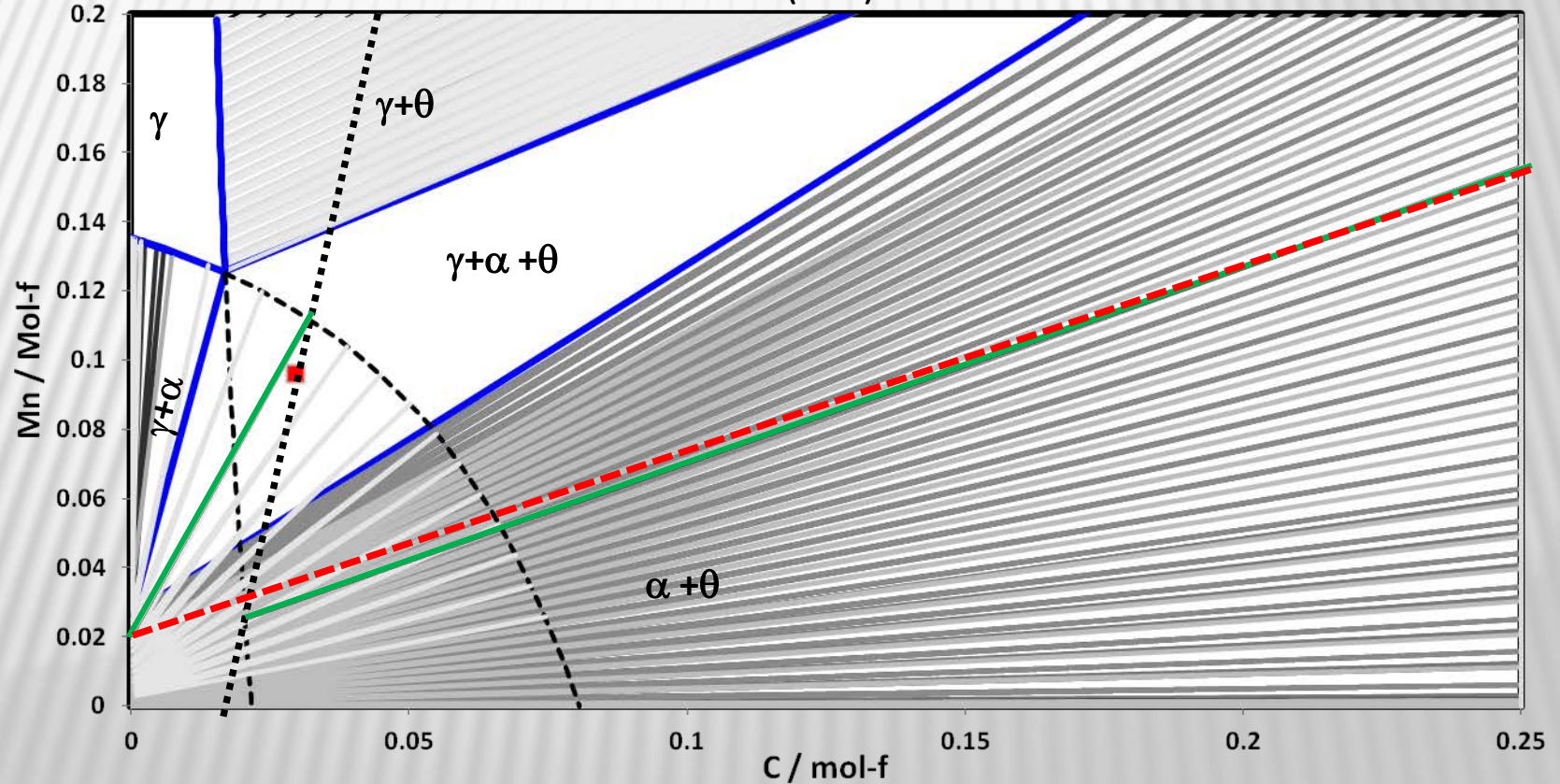
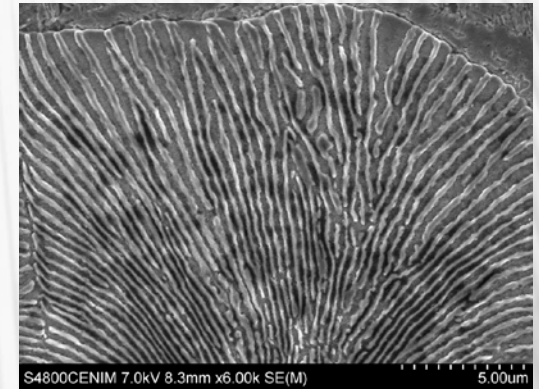
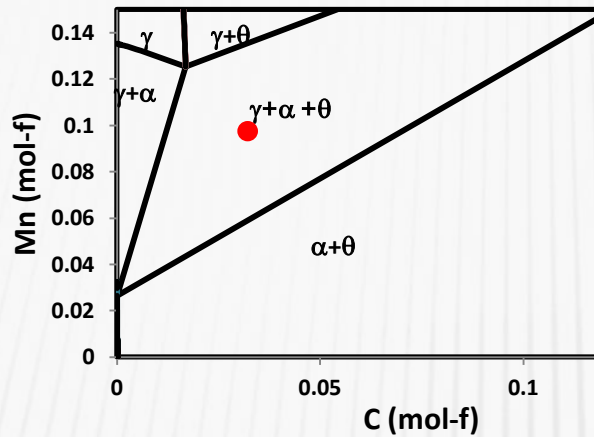
# 5.- COMPOSICIÓN DE LAS FASES

EQ PERLITA CONSTANTE



# 5.- COMPOSICIÓN DE LAS FASES

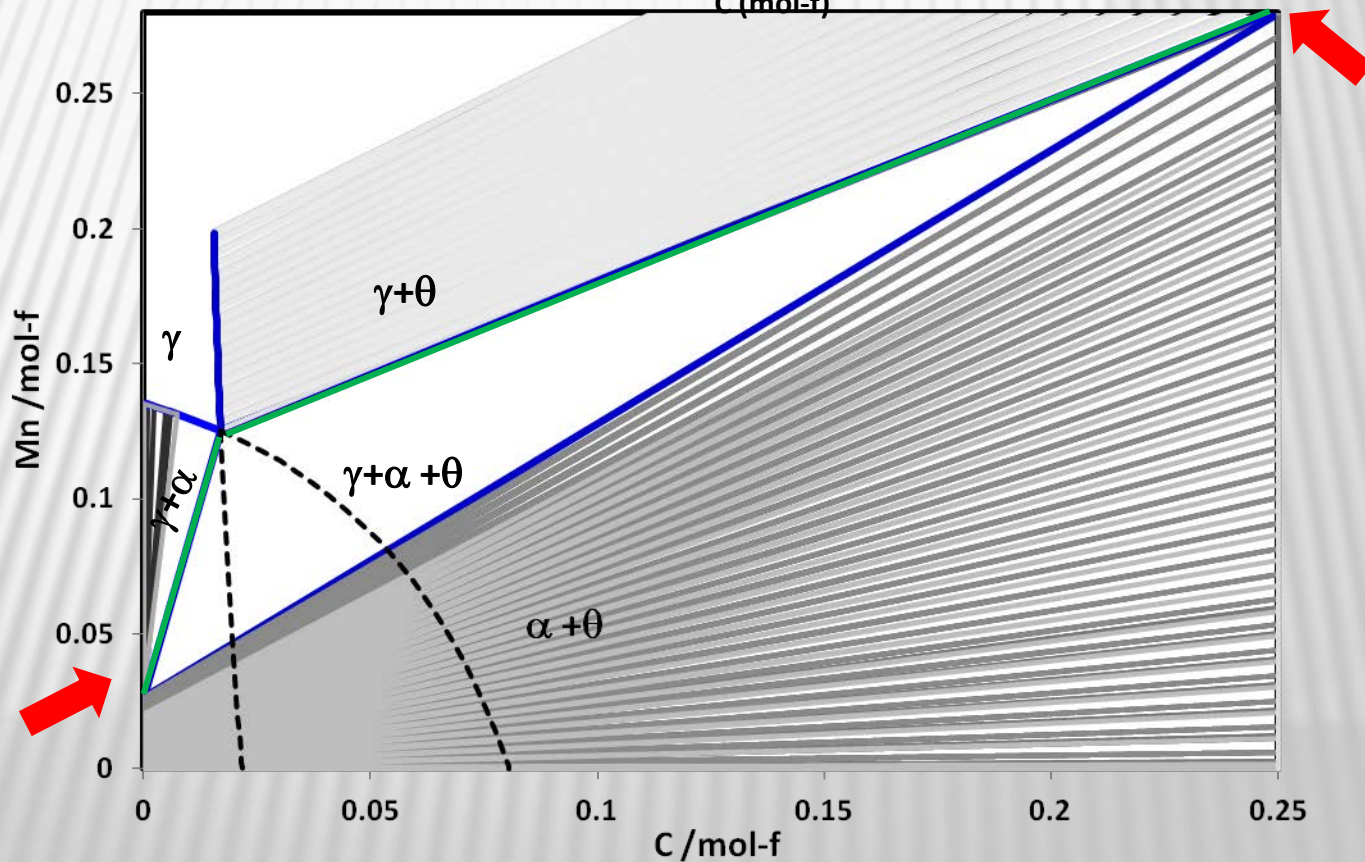
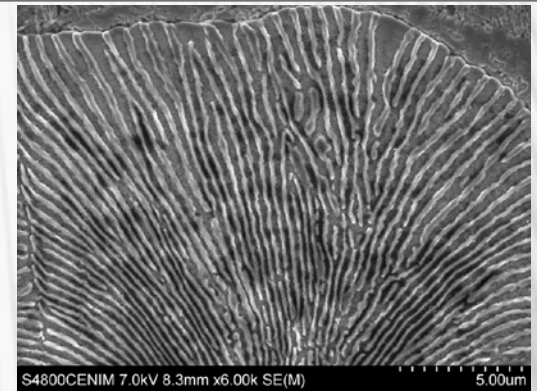
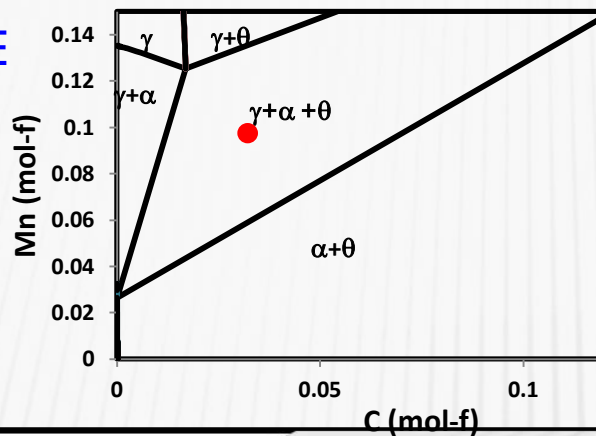
## EL PERLITA DIVERGENTE





# 5.- COMPOSICIÓN DE LAS FASES

## EQ PERLITA DIVERGENTE



!!!GRACIAS POR SU  
ATENCIÓN !!!